# Probe the $\boldsymbol{R}$－Parity Violating Supersymmetry Effects in the $\mathrm{B}_{\mathrm{s}}^{0}-\overline{\mathrm{B}}_{\mathrm{s}}^{0}$ Mixing ${ }^{*}$ 

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#### Abstract

The recent measurements of the $\mathrm{B}_{\mathrm{s}}$ mass difference $\Delta M_{\mathrm{s}}$ by the CDF and $\mathrm{D} \emptyset$ collaborations are roughly consistent with the Standard Model predictions，therefore，these measurements will afford an opportunity to constrain new physics scenarios beyond the Standard Model．We consider the impact of the $R$－ parity violating supersymmetry in the $\mathrm{B}_{\mathrm{s}}^{0}-\overline{\mathrm{B}}_{\mathrm{s}}^{0}$ mixing，and use the latest experimental results of $\Delta M_{\mathrm{s}}$ to constrain the size of the $R$－parity violating tree level couplings in the $\mathrm{B}_{\mathrm{s}}^{0}-\overline{\mathrm{B}}_{\mathrm{s}}^{0}$ mixing．Then，using the constrained RPV parameter space from $\Delta M_{\mathrm{s}}$ ，we show the $R$－parity violating effects on the $\mathrm{B}_{\mathrm{s}}$ width difference $\Delta \Gamma_{\mathrm{s}}$ ．


Key words $\mathrm{B}_{\mathrm{s}}^{0}-\overline{\mathrm{B}}_{\mathrm{s}}^{0}$ mixing，$R$－parity violating，the $\mathrm{B}_{\mathrm{s}}$ mass difference，the $\mathrm{B}_{\mathrm{s}}$ width difference

Recently CDF and DØ collaborations have mea－ sured the mass difference in the $\mathrm{B}_{\mathrm{s}}^{0}-\overline{\mathrm{B}}_{\mathrm{s}}^{0}$ system ${ }^{[1,2]}$ with the results

$$
\begin{align*}
& \mathrm{CDF}: \quad \Delta M_{\mathrm{s}}=\left(17.31_{-0.18}^{+0.33} \pm 0.07\right) / \mathrm{ps}  \tag{1}\\
& \mathrm{D} \emptyset: \quad 17 / \mathrm{ps}<\Delta M_{\mathrm{s}}<21 / \mathrm{ps} \quad(90 \% \text { C.L. }) \tag{2}
\end{align*}
$$

The measurement of CDF collaboration turned out to be surprisingly below the Standard Model （SM）predictions obtained from other constraints ${ }^{[3,4]}$

$$
\begin{align*}
\Delta M_{\mathrm{s}}^{\mathrm{SM}}(\mathrm{UTfit}) & =(21.5 \pm 2.6) / \mathrm{ps}  \tag{3}\\
\Delta M_{\mathrm{s}}^{\mathrm{SM}}(\mathrm{CKMfit}) & =\left(21.7_{-4.2}^{+5.9}\right) / \mathrm{ps}
\end{align*}
$$

A consistent though slightly smaller value is found for the mass difference directly from its SM expression in later Eq．（10）

$$
\begin{equation*}
\Delta M_{\mathrm{s}}^{\mathrm{SM}}(\text { Direct })=(20.8 \pm 6.4) / \mathrm{ps} \tag{4}
\end{equation*}
$$

with the input parameters collected in Table 1．It＇s noted that this prediction is sensitive to the value cho－ sen for the non－perturbative quantity $F_{\mathrm{B}_{\mathrm{s}}} \sqrt{B_{\mathrm{B}_{\mathrm{s}}}}$ and
the CKM matrix element $V_{\text {ts }}$ ，in this paper，we use their values from Refs．［3，5］．The implication of $\Delta M_{\mathrm{s}}$ measurements have already been studied in model in－ dependent approach ${ }^{[6]}$ ，MSSM models ${ }^{[7]}, \mathrm{Z}^{\prime}$－model ${ }^{[8]}$ ， Grand Unified Models ${ }^{[9]}$ ．

The SM prediction in Eq．（4）suffers large uncer－ tainties from the hadronic parameters，nevertheless， the experimental data agree fairly well with the SM value．Therefore，we can use the CDF measurement to constrain new physics which may induce the b－s transition．Effects of the $R$－parity violating（RPV） supersymmetry（SUSY）on the neutral meson mixing have been discussed extensively in Refs．［10，11］．In this paper we will consider the RPV SUSY effects at the tree level in the $\mathrm{B}_{\mathrm{s}}^{0}-\overline{\mathrm{B}}_{\mathrm{s}}^{0}$ mixing by the latest exper－ imental data．Using the latest experimental data of $\Delta M_{\mathrm{s}}$ and the theoretical parameters，we obtain the new bound on the relevant RPV coupling product．If there are RPV contributions to $\Delta M_{\mathrm{s}}$ ，the same new physics will also contribute to the width difference

[^0]$\Delta \Gamma_{\mathrm{s}}$ ，and therefore we will use the constrained pa－ rameter region to examine the RPV effects on $\Delta \Gamma_{\mathrm{s}}$ ．

We first consider the SM contribution to the $\mathrm{B}_{\mathrm{s}}^{0}-\overline{\mathrm{B}}_{\mathrm{s}}^{0}$ mixing．The SM effective Hamiltonian for the $\mathrm{B}_{\mathrm{s}}^{0}-\overline{\mathrm{B}}_{\mathrm{s}}^{0}$ mixing is usually described by ${ }^{[12]}$

$$
\begin{align*}
\mathscr{H}_{\mathrm{eff}}^{\mathrm{SM}}= & \frac{G_{\mathrm{F}}^{2}}{16 \pi^{2}} m_{\mathrm{W}}^{2}\left|V_{\mathrm{ts}}^{*} V_{\mathrm{tb}}\right|^{2} \eta_{2 \mathrm{~B}} S_{0}\left(x_{\mathrm{t}}\right)\left[\alpha_{\mathrm{s}}\left(\mu_{\mathrm{b}}\right)\right]^{-6 / 23} \times \\
& {\left[1+\frac{\alpha_{\mathrm{s}}\left(\mu_{\mathrm{b}}\right)}{4 \pi} J_{5}\right] \mathscr{O}+\text { h.c. } } \tag{5}
\end{align*}
$$

with

$$
\begin{equation*}
\mathscr{O}=(\overline{\mathrm{s}} \mathrm{~b})_{V-A}(\overline{\mathrm{~s}} \mathrm{~b})_{V-A}, \tag{6}
\end{equation*}
$$

where $x_{\mathrm{t}}=m_{\mathrm{t}}^{2} / m_{\mathrm{W}}^{2}$ and $\eta_{2 \mathrm{~B}}$ is the QCD correction．
In terms of Eq．（5），the mixing amplitude $M_{12}^{\mathrm{s}}$ in the SM，dominated by the top quark loop，is

$$
\begin{equation*}
M_{12}^{\mathrm{s}, \mathrm{SM}}=\frac{\left\langle\mathrm{B}_{\mathrm{s}}^{0}\right| \mathscr{H}_{\mathrm{ef}}^{\mathrm{SM}}\left|\overline{\mathrm{~B}}_{\mathrm{s}}^{0}\right\rangle}{2 m_{\mathrm{B}_{\mathrm{s}}}} \tag{7}
\end{equation*}
$$

Defining the renormalization group invariant param－ eter $B_{\mathrm{B}_{\mathrm{s}}}$ by

$$
\begin{gather*}
B_{\mathrm{B}_{\mathrm{s}}}=B_{\mathrm{B}_{\mathrm{s}}}(\mu)\left[\alpha_{\mathrm{s}}(\mu)\right]^{-6 / 23}\left[1+\frac{\alpha_{\mathrm{s}}(\mu)}{4 \pi} J_{5}\right]  \tag{8}\\
\left\langle\mathrm{B}_{\mathrm{s}}^{0}\right| \mathscr{O}\left|\overline{\mathrm{B}}_{\mathrm{s}}^{0}\right\rangle \equiv \frac{8}{3} B_{\mathrm{B}_{\mathrm{s}}}(\mu) F_{\mathrm{B}_{\mathrm{s}}}^{2} m_{\mathrm{B}_{\mathrm{s}}}^{2} \tag{9}
\end{gather*}
$$

then，we have the $\mathrm{B}_{\mathrm{s}}$ mass difference in the SM

$$
\begin{align*}
\Delta M_{\mathrm{s}}^{\mathrm{SM}}= & 2\left|M_{12}^{\mathrm{s}, \mathrm{SM}}\right|=\frac{G_{\mathrm{F}}^{2}}{6 \pi^{2}} m_{\mathrm{W}}^{2} m_{\mathrm{B}_{\mathrm{s}}}\left|V_{\mathrm{ts}}^{*} V_{\mathrm{tb}}\right|^{2} \times \\
& \eta_{2 \mathrm{~B}} S_{0}\left(x_{\mathrm{t}}\right)\left(F_{\mathrm{Bs}_{\mathrm{s}}} \sqrt{B_{\mathrm{B}_{\mathrm{s}}}}\right)^{2} \tag{10}
\end{align*}
$$

In the SM，the off－diagonal element of the decay width matrix $\Gamma_{12}^{\mathrm{s}, \mathrm{SM}}$ may be written as ${ }^{[13]}$

$$
\begin{align*}
\Gamma_{12}^{\mathrm{s}, \mathrm{SM}}= & -\frac{G_{\mathrm{F}}^{2} m_{\mathrm{b}}^{2}}{24 \pi M_{\mathrm{B}_{\mathrm{s}}}}\left|V_{\mathrm{cb}} V_{\mathrm{cs}}^{*}\right|^{2}\left[G\left(x_{\mathrm{c}}\right)\left\langle\mathrm{B}_{\mathrm{s}}^{0}\right| \mathscr{O}\left|\overline{\mathrm{B}}_{\mathrm{s}}^{0}\right\rangle+\right. \\
& \left.G_{2}\left(x_{\mathrm{c}}\right)\left\langle\mathrm{B}_{\mathrm{s}}^{0}\right| \mathscr{O}_{2}\left|\overline{\mathrm{~B}}_{\mathrm{s}}^{0}\right\rangle+\sqrt{1-4 x_{\mathrm{c}}} \hat{\delta}_{1 / m}\right], \tag{11}
\end{align*}
$$

here $x_{\mathrm{c}}=m_{\mathrm{c}}^{2} / m_{\mathrm{b}}^{2}, G\left(x_{\mathrm{c}}\right)=0.030$ and $G_{2}\left(x_{\mathrm{c}}\right)=-0.937$ at the $m_{\mathrm{b}}$ scale ${ }^{[13]}$ ，and the $1 / m_{\mathrm{b}}$ corrections $\hat{\delta}_{1 / m}$ are given in Ref．［14］．The operator $\mathscr{O}$ can be found in Eq．（6），one now encounters a second operator oper－ ator， $\mathscr{O}_{2}$ ，and thereby another B－parameter $B_{2}^{(\mathrm{s})}(\mu)$

$$
\begin{align*}
& \mathscr{O}_{2}=(\overline{\mathrm{s}} \mathrm{~b})_{S-P}(\overline{\mathrm{~s}} \mathrm{~b})_{S-P}, \\
&\left\langle\mathrm{~B}_{\mathrm{s}}^{0}\right| \mathscr{O}_{2}(\mu)\left|\overline{\mathrm{B}}_{\mathrm{s}}^{0}\right\rangle=-\frac{5}{3}\left(\frac{m_{\mathrm{B}_{\mathrm{s}}}}{\bar{m}_{\mathrm{b}}(\mu)+\bar{m}_{\mathrm{s}}(\mu)}\right)^{2} \times \\
& m_{\mathrm{B}_{\mathrm{s}}}^{2} f_{\mathrm{B}_{\mathrm{s}}}^{2} B_{2}^{(\mathrm{s})}(\mu) . \tag{12}
\end{align*}
$$

The width difference between $B_{s}$ mass eigenstates is given by

$$
\begin{align*}
\Delta \Gamma_{\mathrm{s}}^{\mathrm{SM}}= & 2\left|\Gamma_{12}^{\mathrm{s}, \mathrm{SM}}\right|=\frac{G_{\mathrm{F}}^{2} m_{\mathrm{b}}^{2}}{12 \pi M_{\mathrm{B}_{\mathrm{s}}}}\left|V_{\mathrm{cb}} V_{\mathrm{cs}}^{*}\right|^{2} \times \\
& {\left[\frac{8}{3} G\left(x_{\mathrm{c}}\right) B_{\mathrm{B}_{\mathrm{s}}}(\mu) F_{\mathrm{B}_{\mathrm{s}}}^{2} m_{\mathrm{B}_{\mathrm{s}}}^{2}-\frac{5}{3} G_{2}\left(x_{\mathrm{c}}\right) \times\right.} \\
& \left(\frac{m_{\mathrm{B}_{\mathrm{s}}}}{\bar{m}_{\mathrm{b}}(\mu)+\bar{m}_{\mathrm{s}}(\mu)}\right)^{2} m_{\mathrm{B}_{\mathrm{s}}}^{2} f_{\mathrm{B}_{\mathrm{s}}}^{2} B_{2}^{(\mathrm{s})}(\mu)+ \\
& \left.\sqrt{1-4 x_{\mathrm{c}}} \hat{\delta}_{1 / m}\right] \tag{13}
\end{align*}
$$

and the SM predicts $\Delta \Gamma_{\mathrm{s}}^{\mathrm{SM}}$ with the input parameters in Table 1

$$
\begin{equation*}
\Delta \Gamma_{\mathrm{s}}^{\mathrm{SM}}(\text { Direct })=(0.07 \pm 0.03) / \mathrm{ps} \tag{14}
\end{equation*}
$$

It＇s noted that the width difference have been re－ viewed recently in Ref．［15］．

Now we turn to the RPV SUSY contributions to the $\mathrm{B}_{\mathrm{s}}^{0}-\overline{\mathrm{B}}_{\mathrm{s}}^{0}$ mixing．In the most general superpotential of the minimal supersymmetric Standard Model，the RPV superpotential is given by ${ }^{[16]}$

$$
\begin{align*}
\mathscr{W}_{R_{\mathrm{p}}}= & \mu_{i} \hat{L}_{i} \hat{H}_{u}+\frac{1}{2} \lambda_{[i j] k} \hat{L}_{i} \hat{L}_{j} \hat{E}_{k}^{c}+\lambda_{i j k}^{\prime} \hat{L}_{i} \hat{Q}_{j} \hat{D}_{k}^{c}+ \\
& \frac{1}{2} \lambda_{i[j k]}^{\prime \prime} \hat{U}_{i}^{c} \hat{D}_{j}^{c} \hat{D}_{k}^{c} \tag{15}
\end{align*}
$$

where $\hat{L}$ and $\hat{Q}$ are the $S U(2)$－doublet lepton and quark superfields，$\hat{E}^{c}, \hat{U}^{c}$ and $\hat{D}^{c}$ are the singlet su－ perfields，while $i, j$ and $k$ are generation indices and $c$ denotes a charge conjugate field．


Fig．1．The RPV tree level contributions to the $\mathrm{B}_{\mathrm{s}}^{0}-\overline{\mathrm{B}}_{\mathrm{s}}^{0}$ mixing．

The $\lambda^{\prime}$ couplings of Eq．（15）make the $\mathrm{B}_{\mathrm{s}}^{0}-\overline{\mathrm{B}}_{\mathrm{s}}^{0}$ mix－ ing possible at the tree level through the exchange of a sneutrino $\tilde{v}_{i}$ both in the s－and t－channels displayed in Fig．1．The RPV tree level contributions to $\mathrm{B}_{\mathrm{s}}^{0}-\overline{\mathrm{B}}_{\mathrm{s}}^{0}$ mixing are described by

$$
\begin{equation*}
\mathscr{H}_{\mathrm{eff}}^{\mathcal{R}_{\mathrm{p}}}=\frac{1}{4} \sum_{i} \frac{\lambda_{i 32}^{\prime} \lambda_{i 23}^{\prime *}}{m_{\tilde{\mathrm{v}}_{\mathrm{Li}}}^{2}}(\overline{\mathrm{~s} b})_{S-P}(\overline{\mathrm{~s}} \mathrm{~b})_{S+P}+\text { h.c. } \tag{16}
\end{equation*}
$$

where we have a new physics operator

$$
\begin{equation*}
\mathscr{O}_{4}=(\overline{\mathrm{s}} \mathrm{~b})_{S-P}(\overline{\mathrm{~s}} \mathrm{~b})_{S+P} \tag{17}
\end{equation*}
$$

and we define the B－parameter as
$\left\langle\mathrm{B}_{\mathrm{s}}^{0}\right| \hat{\mathscr{O}}_{4}(\mu)\left|\overline{\mathrm{B}}_{\mathrm{s}}^{0}\right\rangle=2\left(\frac{m_{\mathrm{B}_{\mathrm{s}}}}{\bar{m}_{\mathrm{b}}(\mu)+\bar{m}_{\mathrm{s}}(\mu)}\right)^{2} m_{\mathrm{B}_{\mathrm{s}}}^{2} F_{\mathrm{B}_{\mathrm{s}}}^{2} B_{4}^{(\mathrm{s})}(\mu)$.
Note that the expectation values are scaled by factor of $2 m_{\mathrm{B}}$ over those given in some literature due to our different normalization of the meson wave functions． It is trivial to check that both conventions yield the same values for physical observables．

The RPV mixing amplitude $M_{12}^{\mathrm{s}, R_{\mathrm{p}}}$ is

$$
\begin{align*}
M_{12}^{\mathrm{s}, R_{\mathrm{p}}}= & \frac{\left\langle\mathrm{B}_{\mathrm{s}}^{0}\right| \mathscr{H}_{\mathrm{eff}}^{R_{\mathrm{p}}}\left|\overline{\mathrm{~B}}_{\mathrm{s}}^{0}\right\rangle}{2 m_{\mathrm{B}_{\mathrm{s}}}}=\sum_{i} \frac{\lambda_{i 32}^{\prime} \lambda_{i 23}^{\prime *}}{m_{\bar{v}_{\mathrm{Li}}}} \frac{1}{4} \times \\
& \left(\frac{m_{\mathrm{B}_{\mathrm{s}}}}{\bar{m}_{\mathrm{b}}(\mu)+\bar{m}_{\mathrm{s}}(\mu)}\right)^{2} m_{\mathrm{B}_{\mathrm{s}}} F_{\mathrm{B}_{\mathrm{s}}}^{2} B_{4}^{(\mathrm{s})}(\mu), \tag{19}
\end{align*}
$$

Given the expressions above，we now write the total $\mathrm{B}_{\mathrm{s}}$ mass difference included both SM and RPV contributions

$$
\begin{equation*}
\Delta M_{\mathrm{s}}=2\left|M_{12}^{\mathrm{s}}\right| \tag{20}
\end{equation*}
$$

with

$$
\begin{equation*}
M_{12}^{\mathrm{s}}=M_{12}^{\mathrm{s}, \mathrm{SM}}+M_{12}^{\mathrm{s}, K_{\mathrm{p}}}=M_{12}^{\mathrm{s}, \mathrm{SM}}\left(1+z \mathrm{e}^{\mathrm{i} \theta}\right) \tag{21}
\end{equation*}
$$

where the parameters $z$ and $\theta$ give the relative mag－ nitude and relative phase of the RPV contribution， i．e．$z \equiv\left|M_{12}^{\mathrm{s} R_{\mathrm{p}}} / M_{12}^{\mathrm{s}, \mathrm{SM}}\right|$ and $\theta \equiv \arg \left(M_{12}^{\mathrm{s}, \mathcal{R}_{\mathrm{p}}} / M_{12}^{\mathrm{s}, \mathrm{SM}}\right)$ ．

The $\mathrm{B}_{\mathrm{s}}$ width difference beyond the SM has been studied in Refs．［17，18］．If there are RPV contribu－ tions to $\Delta M_{\mathrm{s}}$ ，the same new physics will also con－ tribute to the $\mathrm{B}_{\mathrm{s}}$ width difference．The width differ－ ence including the RPV contributions is given by ${ }^{[18]}$

$$
\begin{equation*}
\Delta \Gamma_{\mathrm{s}}=\frac{4\left|\operatorname{Re}\left(M_{12}^{\mathrm{s}} \Gamma_{12}^{\mathrm{s} *}\right)\right|}{\Delta M_{\mathrm{s}}}=2\left|\Gamma_{12}^{\mathrm{s}}\right| \cdot\left|\cos \phi_{\mathrm{m}}\right| \tag{22}
\end{equation*}
$$

where $\phi_{\mathrm{m}}=\arg \left(1+z \mathrm{e}^{\mathrm{i} \theta}\right)$ ，and $\phi_{\mathrm{m}}=0$ turns out to be an excellent approximation in the SM．The effect of NP on the off－diagonal element of the decay width $\operatorname{matrix} \Gamma_{12}^{\mathrm{s}}$ is anticipated to be negligibly small，hence $\Gamma_{12}^{\mathrm{s}}=\Gamma_{12}^{\mathrm{s}, \mathrm{SM}}$ is held as a good approximation ${ }^{[19]}$ ．

We now perform numerical calculation and show the constraint imposed by the measurement of $\Delta M_{\mathrm{s}}$ only or both $\Delta M_{\mathrm{s}}$ and $\Delta \Gamma_{\mathrm{s}}$ ．The values of the input parameters used in this paper are collected in Table 1，
and we will use the input parameters and the experi－ mental data which vary randomly within $1 \sigma$ variance．

Table 1．Values of the theoretical quantities as input parameters．

| $m_{\mathrm{W}}=80.403 \pm 0.029 \mathrm{GeV}, m_{\mathrm{B}_{\mathrm{s}}}=5.3696 \pm 0.0024 \mathrm{GeV}$, |  |
| :--- | ---: |
| $\bar{m}_{\mathrm{b}}\left(\bar{m}_{\mathrm{b}}\right)=4.20 \pm 0.07 \mathrm{GeV}, \bar{m}_{\mathrm{s}}(2 \mathrm{GeV})=0.095 \pm 0.025 \mathrm{GeV}$, |  |
| $m_{\mathrm{t}}=174.2 \pm 3.3 \mathrm{GeV}, m_{\mathrm{b}}=4.8 \mathrm{GeV}$. | Ref．$[20]$ |
| $A=0.818_{-0.017}^{+0.007}, \lambda=0.2272 \pm 0.0010$. | Ref．［20］ |
| $\eta_{2 \mathrm{~B}}=0.55 \pm 0.01$. | Ref．［21］ |
| $F_{\mathrm{B}_{\mathrm{s}}} \sqrt{B_{\mathrm{B}_{\mathrm{s}}}}=0.262 \pm 0.035 \mathrm{GeV}$, |  |
| $F_{\mathrm{B}_{\mathrm{s}}}=0.230 \pm 0.030 \mathrm{GeV}$. | Ref．［5］ |
| $B_{2}^{(\mathrm{s})}\left(m_{\mathrm{b}}\right)=0.832 \pm 0.004$, |  |
| $B_{4}^{(\mathrm{s})}\left(m_{\mathrm{b}}\right)=1.172_{-0.007}^{+0.005}$. | Ref．［22］ |

We calculate the contributions of Eq．（16）to $\Delta M_{\mathrm{s}}$ and require it not to exceed the corresponding exper－ imental data in Eq．（1）．The random variation of the parameters subjecting to the constraint leads to the scatter plot shown in Fig． 2.


Fig．2．Allowed parameter space for $\lambda_{i 32}^{\prime} \lambda_{i 23}^{\prime *}$ constrained by the experimental data of $\Delta M_{\mathrm{s}}$ ．

We can see that there are three possible bands of solutions in Fig．2．The two bands are for the modulus of RPV weak phase $\left(\phi_{R_{\mathrm{p}}}\right) \in\left[\frac{5}{9} \pi, \pi\right]$ and $\left|\lambda_{i 32}^{\prime} \lambda_{i 23}^{\prime *}\right| \leqslant 3.2 \times 10^{-7}$ ．The other band is for $\phi_{R_{\mathrm{p}}} \in$ $[-\pi, \pi]$ and $\left|\lambda_{i 32}^{\prime} \lambda_{i 23}^{\prime *}\right| \leqslant 1.4 \times 10^{-6},\left|\phi_{R_{\mathrm{p}}}\right|$ is increasing with $\left|\lambda_{i 32}^{\prime} \lambda_{i 23}^{\prime *}\right|$ in this band．We get a very strong bound on the magnitudes of the RPV coupling prod－ uct $\lambda_{i 32}^{\prime} \lambda_{i 23}^{\prime *}$ from $\Delta M_{\mathrm{s}}$

$$
\begin{equation*}
\left|\lambda_{i 32}^{\prime} \lambda_{i 23}^{\prime *}\right| \leqslant 1.4 \times 10^{-6} \times\left(\frac{100 \mathrm{GeV}}{m_{\tilde{v}_{\mathrm{i}}}}\right)^{2} \tag{23}
\end{equation*}
$$

For comparison，we will use the existing bounds on these single coupling in Refs．［23－25］to compose the corresponding bounds on the quadric coupling prod－ ucts with the superpartner mass being 100 GeV ．In the RPV SUSY model，the strongest bound for this coupling is $\left|\lambda_{i 32}^{\prime} \lambda_{i 23}^{\prime *}\right| \leqslant 1.4 \times 10^{-3}$ in Ref．［23］，and
some bounds are obtained $\left|\lambda_{132}^{\prime} \lambda_{123}^{\prime *}\right| \leqslant 1.0 \times 10^{-11}$ and $\left|\lambda_{232}^{\prime} \lambda_{223}^{\prime *}\right| \leqslant 1.0 \times 10^{-3}$ by the experimental upper lim－ its on the electric dipole moment＇s of the fermions in Ref．［24］．In addition，in the RPV mSUGRA model， Allanach et al．have obtained quite strong upper bound：$\left|\lambda_{i 32}^{\prime} \lambda_{i 23}^{\prime *}\right| \leqslant 2.6 \times 10^{-9}$ at the $M_{\text {GUT }}$ scale and $\left|\lambda_{i 32}^{\prime} \lambda_{i 23}^{\prime *}\right| \leqslant 2.2 \times 10^{-8}$ at the $M_{\mathrm{Z}}$ scale ${ }^{[25]}$ ，so their con－ straints from neutrino masses are stronger than ours from the $\mathrm{B}_{\mathrm{s}}^{0}-\overline{\mathrm{B}}_{\mathrm{s}}^{0}$ mixing．However，we note that the constraints on $\lambda^{\prime}$ from neutrino masses would depend on the explicit neutrino mass models with trilinear couplings only，bilinear couplings only，or both ${ }^{[23]}$ ．

Using the constrained parameter space from $\Delta M_{\mathrm{s}}$ as shown in Fig．2，one can predict the RPV effects on the $\mathrm{B}_{\mathrm{s}}$ width difference $\Delta \Gamma_{\mathrm{s}}$ ．Our predictions of $\Delta \Gamma_{\mathrm{s}}$ are displayed in Fig．3．From Fig．3（a），we find that $\phi_{\mathrm{m}}$ can have any value from $-\pi$ to $\pi$ ，as discussed in Ref．［18］，the RPV contributions to the mixing could reduce $\Delta \Gamma_{\mathrm{s}}$ relative to the SM prediction，and $\Delta \Gamma_{\mathrm{s}}$ lies between $0.00 /$ ps and $0.10 / \mathrm{ps}$ ．We present correla－ tion between $\Delta \Gamma_{\mathrm{s}}$ and the parameter space of $\lambda_{i 32}^{\prime} \lambda_{i 23}^{\prime *}$ by the three－dimensional scatter plot in Fig．3（b）．We also give projections on three vertical planes，where the $\left|\lambda_{i 32}^{\prime} \lambda_{i 23}^{\prime *}\right|-\phi_{R_{\mathrm{p}}}$ plane displays the constrained re－ gion of $\lambda_{i 32}^{\prime} \lambda_{i 23}^{\prime *}$ as the plot of Fig．2．It＇s shown that $\Delta \Gamma_{\mathrm{s}}$ is decreasing first and then increasing with $\left|\lambda_{i 32}^{\prime} \lambda_{i 23}^{\prime *}\right|$ on the $\Delta \Gamma_{\mathrm{s}}-\left|\lambda_{i 32}^{\prime} \lambda_{i 23}^{\prime *}\right|$ plane．From the $\Delta \Gamma_{\mathrm{s}^{-}}$ $\phi_{R_{\mathrm{p}}}$ plane，we can see that $\Delta \Gamma_{\mathrm{s}}$ may be reduced to zero when $\left|\phi_{R_{\mathrm{p}}}\right|$ lies in $\left[\frac{2}{3} \pi, \frac{8}{9} \pi\right]$ ．


Fig．3．The RPV tree level contributions to the $\Delta \Gamma_{\mathrm{s}}$ ．
The present experimental data of the $B_{s}$ width dif－ ference have a large error，and we obtain the averaged value from ${ }^{[20,26]}$

$$
\begin{equation*}
\Delta \Gamma_{\mathrm{s}}=(0.22 \pm 0.09) / \mathrm{ps} \tag{24}
\end{equation*}
$$

Now we add the experimental constraint of $\Delta \Gamma_{\mathrm{s}}$ to the allowed space of $\lambda_{i 32}^{\prime} \lambda_{i 23}^{\prime *}$ ．We can not get the solution
to the experimental data of $\Delta \Gamma_{\mathrm{s}}$ at $1 \sigma$ level．If $\Delta \Gamma_{\mathrm{s}}$ is varied randomly within $2 \sigma$ variance，we can obtain the scatter plot as exhibited in Fig．4．Comparing Fig． 4 with Fig．2，we can see that the experimental bound on $\Delta \Gamma_{\mathrm{s}}$ shown in Eq．（24）obviously excludes the region $4.4 \times 10^{-7}<\left|\lambda_{i 32}^{\prime} \lambda_{i 23}^{\prime *}\right|<5.5 \times 10^{-7}$ ．The stronger limit on $\left|\lambda_{i 32}^{\prime} \lambda_{i 23}^{\prime *}\right|$ from $\Delta M_{\mathrm{s}}$ and $\Delta \Gamma_{\mathrm{s}}$ than the one from $\Delta M_{\mathrm{s}}$ only is obtained

$$
\begin{equation*}
\left|\lambda_{i 32}^{\prime} \lambda_{i 23}^{\prime *}\right| \leqslant 4.4 \times 10^{-7} \times\left(\frac{100 \mathrm{GeV}}{m_{\tilde{v}_{\mathrm{i}}}}\right)^{2} \tag{25}
\end{equation*}
$$

and

$$
\begin{equation*}
\left|\lambda_{i 32}^{\prime} \lambda_{i 23}^{\prime *}\right| \in[5.5,13.1] \times 10^{-7} \times\left(\frac{100 \mathrm{GeV}}{m_{\widetilde{v}_{\mathrm{i}}}}\right)^{2} \tag{26}
\end{equation*}
$$



Fig．4．Allowed parameter space for $\lambda_{i 32}^{\prime} \lambda_{i 23}^{\prime *}$ constrained by the data of $\Delta M_{\mathrm{s}}$ and $\Delta \Gamma_{\mathrm{s}}$ ．

In summary，we have studied the RPV tree level effects in the $\mathrm{B}_{\mathrm{s}}^{0}-\overline{\mathrm{B}}_{\mathrm{s}}^{0}$ mixing with the current experi－ mental measurements．As shown，using the latest ex－ perimental data of $\Delta M_{\mathrm{s}}$ and the theoretical parame－ ters，we have obtained the allowed space of the RPV coupling product $\lambda_{i 32}^{\prime} \lambda_{i 23}^{\prime *}$ ，the upper bound on the magnitude of $\lambda_{i 32}^{\prime} \lambda_{i 23}^{\prime *}$ has been greatly improved over the existing bounds obtained from the RPV SUSY． Then，we have examined the RPV effects on $\Delta \Gamma_{\mathrm{s}}$ by the constrained region of $\lambda_{i 32}^{\prime} \lambda_{i 23}^{*}$ from $\Delta M_{\mathrm{s}}$ ，and we have found that the RPV contributions to the mixing could reduce $\Delta \Gamma_{\mathrm{s}}$ relative to the SM prediction．Fi－ nally，using the experimental data of $\Delta M_{\mathrm{s}}$ and $\Delta \Gamma_{\mathrm{s}}$ ， we have obtained stronger bound than the one from $\Delta M_{\mathrm{s}}$ only on $\lambda_{i 32}^{\prime} \lambda_{i 23}^{\prime *}$ ．In addition，we stress that once LHC is turned on，with the anticipated production of $10^{12} \mathrm{~b} \overline{\mathrm{~b}}$ per year，the measurements of $\Delta M_{\mathrm{s}}$ and $\Delta \Gamma_{\mathrm{s}}$ will be much more accurate，then the allowed param－ eter space for $\lambda_{i 32}^{\prime} \lambda_{i 23}^{\prime *}$ will be significantly shrunken or ruled out．

## References

1 CDF Collaboration（Abulencia A et al．）．hep－ex／0606027
D D Collaboration（Abazov V M et al．）．hep－ex／0603029
3 CKMfitter Group（Charles J et al．）．Eur．Phys．J．， 2005，C41：1，updated results and plots available at： http：／／ckmfitter．in2p3．fr／
4 UTfit Collaboration（Bona M et al．）．JHEP，2006，0603： 080
5 Hashimoto S．Int．J．Mod．Phys．，2005，A20： 5133
6 Blanke M，Buras A J，Guadagnoli D et al．hep－ph／0604057； Ball P，Fleischer R．hep－ph／0604249；Ligeti Z，Papucci M， Perez G．hep－ph／0604112；Grossman Y，Nir Y，Raz G． hep－ph／0605028；UTfit Collaboration（Bona M et al．）．hep－ ph／0605213
7 Ciuchini M，Silvestrini L．hep－ph／0603114；Foster J，Oku－ mura K I，Roszkowski L．hep－ph／0604121；Khalil S．hep－ ph／0605021；Endo M，Mishima S．hep－ph／0603251；Baek S． hep－ph／0605182；Isidori G，Paradisi P．Phys．Lett．，2006， B639： 499
8 Cheung K et al．hep－ph／0604223；HE Xiao－Gang，Valen－ cia G．hep－ph／0605202；Baek S，Jeon Jong Hun，Kim C S． hep－ph／0607113
9 Dutta B，Mimura Y．hep－ph／0607147；Parry J K．hep－ ph／0606150；Parry J K．hep－ph／0608192
10 Nandi S，Saha J P．hep－ph／0608341；Saha J P，Kundu A． Phys．Rev．，2004，D69：016004；Kundu A，Saha J P．Phys． Rev．，2004，D70：096002；Bhattacharyya G，Raychaudhuri A．Phys．Rev．，1998，D57：3837；Choudhury D，Roy Pro－ bir．Phys．Lett．，1996，B378：153；Agashe K，Graesser M． Phys．Rev．，1996，D54： 4445

11 Carlos B de，White P．Phys．Rev．，1997，D55：4222；Guetta D．Phys．Rev．，1998，D58： 116008
12 Buchalla G，Buras A J，Lauteubacher M E．Rev．Mod． Phys．，1996，68： 1125
13 Beneke M et al．Phys．Lett．，1999，B459：631；Lenz A． hep－ph／9906317
14 Beneke M，Buchalla G，Dunietz I．Phys．Rev．，1996，D54： 4419
15 Lenz A．hep－ph／0412007
16 Weinberg S．Phys．Rev．，1982，D26： 287
17 XING Zhi－Zhong．Eur．Phys．J．，1998，C4： 283
18 Grossman Y．Phys．Lett．，1996，B380： 99
19 Bigi I I，Khoze V A，Uraltsev N G et al．In CP Viola－ tion，Edited by Jarlskog C，Singapore：World Scientific， 1988．175；Hewett J L，Takeuchi T，Thomas S．SLAC－PUB－ 7088 or CERN－TH／96－56；Grossman Y，Nir Y，Rattazzi R． SLAC－PUB－7379 or CERN－TH－96－368；Gronau M，London D．Phys．Rev．，1997，D55： 2845
20 YAO W M et al．Journal of Physics，2006，G33： 1
21 Buras A J，Jamin M，Weisz P H．Nucl．Phys．，1990，B347： 491；Urban J et al．Nucl．Phys．，1998，B523： 40
22 Bećirević D et al．J．High Energy Physics，2002，0204： 025
23 Barbier R et al．Phys．Rept．，2005，420：1；Chemtob M． Prog．Part．Nucl．Phys．，2005，54： 71
24 Frank M，Hamidian H．J．Phys．，1998，G24： 2203
25 Allanach B C，Dedes A，Dreiner H K．Phys．Rev．，2004， D69： 115002
26 D $\emptyset$ Collaboration（Abazov V M et al．）．Phys．Rev．Lett．， 2005，95：171801；CDF Collaboration（Acosta D et al．）． Phys．Rev．Lett．，2005，94：101803；ALEPH Collabora－ tion（Barate R et al．）．Phys．Lett．，2000，B486： 286

# 探测 $\mathrm{B}_{\mathrm{s}}^{0}-\overline{\mathrm{B}}_{\mathrm{s}}^{0}$ 混合中的 $\boldsymbol{R}$ 宇称破缺超对称效应＊ 

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#### Abstract

摘要 最近由 CDF 合作组和 $\mathrm{D} \varnothing$ 合作组测量的 $\mathrm{B}_{\mathrm{s}}$ 质量差 $\Delta M_{\mathrm{s}}$ 粗略地与标准模型预测值一致，因此这些测量将对限制超出标准模型的新物理信号提供一个机会。考虑 $\mathrm{B}_{\mathrm{s}}^{0}-\overline{\mathrm{B}}_{\mathrm{s}}^{0}$ 混合中的 $R$ 宇称破缺超对称效应，并用最近 $\Delta M_{\mathrm{s}}$的实验结果去限制树图的 $R$ 宇称破缺耦合。然后，通过从 $\Delta M_{\mathrm{s}}$ 实验限制得到 $R$ 宇称破缺耦合的参数空间，显示在 $\mathrm{B}_{\mathrm{s}}$ 宽度差 $\Delta \Gamma_{\mathrm{s}}$ 中的 $R$ 宇称破缺超对称效应。


关键词 $\mathrm{B}_{\mathrm{s}}^{0}-\overline{\mathrm{B}}_{\mathrm{s}}^{0}$ 混合 $R$ 宇称破缺 $\mathrm{B}_{\mathrm{s}}$ 质量差 $\mathrm{B}_{\mathrm{s}}$ 宽度差

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