

95 GeV Higgs boson and nano-Hertz gravitational waves from domain walls in the N2HDM*

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Abstract: We explore the diphoton and $b\bar{b}$ excesses at 95.4 GeV, as well as nano-Hertz gravitational waves originating from domain walls, within the framework of the next-to-two-Higgs-doublet model (N2HDM), which extends the two-Higgs-doublet model by introducing a real singlet scalar subject to a discrete Z_2 symmetry. The Z_2 symmetry is spontaneously broken by the non-zero vacuum expectation value of the singlet scalar, v_s , which leads to the formation of domain walls. We discuss two different scenarios: in scenario A, the 95.4 GeV Higgs boson predominantly originates from the singlet field, while in scenario B, it arises mainly from the CP-even components of the Higgs doublets. Taking into account relevant theoretical and experimental constraints, we find that scenario A can fully account for both the diphoton and $b\bar{b}$ excesses at 95.4 GeV within the 1σ range. In the parameter space accommodating both excesses, scenario A fails to provide a valid explanation for the NANOGrav data up to $v_s = 1000$ TeV, and the predicted gravitational wave spectrum can exceed the SKA sensitivity curve in the low frequency region. Scenario B only marginally accounts for the diphoton and $b\bar{b}$ excesses at the 1σ level, but it can simultaneously explain the NANOGrav data well.

Keywords: N2HDM, Higgs boson, domain walls

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I. INTRODUCTION

The possibility of additional Higgs states beyond the Standard Model (SM) is an open question. The emergence of experimental anomalies hinting at a scalar resonance around 95.4 GeV has generated significant interest within the high-energy physics community. Hints of a light scalar near 95.4 GeV first appeared in searches at LEP collider, where a 2.3σ excess in the $e^+e^- \rightarrow Z\phi$ process with $\phi \rightarrow b\bar{b}$ was reported [1]. Recently, the CMS collaboration has observed a local significance of 2.9σ in the diphoton invariant mass spectrum around 95.4 GeV using full Run 2 data set of LHC [2]. The ATLAS experiment has also observed an excess in the diphoton channel, albeit with a lower significance [3]. Neglecting possible correlations, the combined signal strength of ATLAS and CMS has a 3.1σ local excess in the diphoton channel around 95.4 GeV [4]. There are numerous explanations on the excesses in the new physics models, for example Refs. [4–62].

On the other hand, current observations from several

pulsar timing array (PTA) collaborations have yielded strong statistical evidence for a stochastic gravitational wave background (SGWB) in the nano-Hertz regime, including NANOGrav [63,64], the European Pulsar Timing Array (EPTA) [65,66], the Parkes Pulsar Timing Array (PPTA) [67], and the Chinese Pulsar Timing Array (CPTA) [68]. In addition to the supermassive black hole binaries interpretation [69], there are various cosmological sources of the gravitational waves (GWs), such as cosmic strings [70–80], domain walls [81–93], primordial first-order phase transitions [94–115], and inflation [116–127].

In this paper, we explore the possibility of simultaneously explaining the observed excess of 95.4 GeV Higgs boson and the nano-Hertz SGWB within the framework of the two-Higgs-doublet model extended by a real singlet scalar, commonly referred to as the N2HDM [6–8,128–130]. In this model, the 95.4 GeV Higgs boson arises from the mixing among three CP-even scalar fields, including the singlet field. In addition, the N2HDM respects a discrete Z_2 symmetry, which is spontaneously

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broken by the non-zero vacuum expectation value (VEV) of the singlet scalar. The spontaneous breaking of this discrete Z_2 symmetry in the early Universe leads to the formation of domain walls that separate regions of distinct vacua. The authors of [131] studied the possibility of restoring the electroweak symmetry in the N2HDM via the domain walls. To ensure that the domain walls are unstable and eventually annihilate, the discrete symmetry is explicitly broken by introducing a very small bias term. The peak frequency of GWs produced by the domain walls is set by the time of annihilation, while the amplitude depends on the energy density of domain wall. This model has the potential to generate domain walls whose dynamics may produce GWs in the nano-Hertz frequency band, offering a possible explanation for the NANOGrav data.

The remainder of this paper is organized as follows. In Section II we present the key features of the N2HDM. In Sections III and IV, we examine the relevant theoretical and experimental constraints, and discuss the explanation of the diphoton and $b\bar{b}$ excesses at 95.4 GeV. In Section V we explore the domain walls and the associated GW spectra. Finally, we summarize our conclusions in Section VI.

II. THE MODEL

The two-Higgs-doublet model is extended by introducing a real singlet scalar,

$$\Phi_1 = \begin{pmatrix} \phi_1^+ \\ \frac{(v_1 + \rho_1 + i\eta_1)}{\sqrt{2}} \end{pmatrix}, \Phi_2 = \begin{pmatrix} \phi_2^+ \\ \frac{(v_2 + \rho_2 + i\eta_2)}{\sqrt{2}} \end{pmatrix},$$

$$\Phi_S = \rho_s + v_s, \quad (1)$$

After spontaneous symmetry breaking, the fields Φ_1, Φ_2 and Φ_S acquire their VEVs v_1, v_2 , and v_s , with $v \equiv \sqrt{v_1^2 + v_2^2} = 246$ GeV. The ratio of the two-Higgs-doublet VEVs is defined as $\tan\beta \equiv v_2/v_1$.

The Higgs potential is written as

$$\begin{aligned} V = & m_{11}^2 |\Phi_1|^2 + m_{22}^2 |\Phi_2|^2 - m_{12}^2 (\Phi_1^\dagger \Phi_2 + \text{h.c.}) \\ & + \frac{\lambda_1}{2} (\Phi_1^\dagger \Phi_1)^2 + \frac{\lambda_2}{2} (\Phi_2^\dagger \Phi_2)^2 \\ & + \lambda_3 (\Phi_1^\dagger \Phi_1)(\Phi_2^\dagger \Phi_2) + \lambda_4 (\Phi_1^\dagger \Phi_2)(\Phi_2^\dagger \Phi_1) \\ & + \frac{\lambda_5}{2} [(\Phi_1^\dagger \Phi_2)^2 + \text{h.c.}] + \frac{m_s^2}{2} \Phi_S^2 + \frac{\lambda_6}{8} \Phi_S^4 \\ & + \frac{\lambda_7}{2} (\Phi_1^\dagger \Phi_1) \Phi_S^2 + \frac{\lambda_8}{2} (\Phi_2^\dagger \Phi_2) \Phi_S^2. \end{aligned} \quad (2)$$

We assume that the model conserves CP-symmetry,

meaning all coupling constants and mass parameters to be real. The Higgs potential in Eq. (2) respects a discrete Z_2 symmetry,

$$\Phi_1 \rightarrow \Phi_1, \Phi_2 \rightarrow \Phi_2, \Phi_S \rightarrow -\Phi_S, \quad (3)$$

which is spontaneously broken by the VEV of Φ_S , giving rise to domain walls in the early Universe. The conditions for minimizing the scalar potential lead to

$$v_2 m_{12}^2 - v_1 m_{11}^2 = \frac{1}{2} (v_1^3 \lambda_1 + v_2^2 v_1 \lambda_{345} + v_s^2 v_1 \lambda_7), \quad (4)$$

$$v_1 m_{12}^2 - v_2 m_{22}^2 = \frac{1}{2} (v_1^2 v_2 \lambda_{345} + v_2^3 \lambda_2 + v_s^2 v_2 \lambda_8), \quad (5)$$

$$-v_s m_s^2 = \frac{1}{2} v_s (v_1^2 \lambda_7 + v_2^2 \lambda_8 + v_s^2 \lambda_6), \quad (6)$$

where $\lambda_{345} \equiv \lambda_3 + \lambda_4 + \lambda_5$.

It is necessary to introduce an energy bias in the potential, which lifts the degenerate minima connected by the discrete Z_2 symmetry. This bias destabilizes the domain walls, thereby evading the associated cosmological constraints [132–134]. Here we introduce the Z_2 symmetry-breaking potential term by hand,

$$V_{Z_2} = -a_1 v_s^2 \Phi_S + \frac{a_1}{3} \Phi_S^3. \quad (7)$$

The total potential still has minima at $(v_1, v_2, \pm v_s)$, but there is an energy difference between them

$$V_{\text{bias}} = V(v_1, v_2, -v_s) - V(v_1, v_2, v_s) = \frac{4}{3} a_1 v_s^3. \quad (8)$$

In fact, since the required values of a_1 is extremely small, we only consider it in the discussions of domain walls, and neglect it in other calculations.

Once spontaneous symmetry breaking occurs, the mass eigenstates are derived from the original fields through the application of rotation matrices

$$\begin{pmatrix} h_1, h_2, h_3 \end{pmatrix} = \begin{pmatrix} \rho_1, \rho_2, \rho_s \end{pmatrix} R^T, \quad (9)$$

$$\begin{pmatrix} G^0 \\ A \end{pmatrix} = \begin{pmatrix} \cos\beta & \sin\beta \\ -\sin\beta & \cos\beta \end{pmatrix} \begin{pmatrix} \eta_1 \\ \eta_2 \end{pmatrix}, \quad (10)$$

$$\begin{pmatrix} G^\pm \\ H^\pm \end{pmatrix} = \begin{pmatrix} \cos\beta & \sin\beta \\ -\sin\beta & \cos\beta \end{pmatrix} \begin{pmatrix} \phi_1^\pm \\ \phi_2^\pm \end{pmatrix}, \quad (11)$$

with

$$R = \begin{pmatrix} c_1 c_2 & s_1 c_2 & s_2 \\ -s_1 c_3 - c_1 s_2 s_3 & c_1 c_3 - s_1 s_2 s_3 & c_2 s_3 \\ s_1 s_3 - c_1 s_2 c_3 & -s_1 s_2 c_3 - c_1 s_3 & c_2 c_3 \end{pmatrix}. \quad (12)$$

The shorthand notations are $s_{1,2,3} \equiv \sin \alpha_{1,2,3}$ and $c_{1,2,3} \equiv \cos \alpha_{1,2,3}$. The G^0 and $G^\pm$ correspond to the Goldstone bosons, which are absorbed by the Z and $W^\pm$. The remaining physical states consist of three CP-even scalars $h_{1,2,3}$, one pseudoscalars A , and a pair of charged scalars $H^\pm$.

The coupling constants in the Higgs potential can be expressed in terms of the scalar masses and mixing angles as

$$\begin{aligned} \lambda_1 &= \frac{m_{h_1}^2 R_{11}^2 + m_{h_2}^2 R_{21}^2 + m_{h_3}^2 R_{31}^2 - m_{12}^2 t_\beta}{v^2 c_\beta^2}, \\ \lambda_2 &= \frac{m_{h_1}^2 R_{12}^2 + m_{h_2}^2 R_{22}^2 + m_{h_3}^2 R_{32}^2 - m_{12}^2 t_\beta^{-1}}{v^2 s_\beta^2}, \\ \lambda_3 &= \frac{m_{h_1}^2 R_{11} R_{12} + m_{h_2}^2 R_{21} R_{22} + m_{h_3}^2 R_{31} R_{32} + 2m_{H^\pm}^2 s_\beta c_\beta - m_{12}^2}{v^2 s_\beta c_\beta}, \\ \lambda_4 &= \frac{(m_A^2 - 2m_{H^\pm}^2) s_\beta c_\beta + m_{12}^2}{v^2 s_\beta c_\beta}, \\ \lambda_5 &= \frac{-m_A^2 s_\beta c_\beta + m_{12}^2}{v^2 s_\beta c_\beta}, \\ \lambda_6 &= \frac{m_{h_1}^2 R_{13}^2 + m_{h_2}^2 R_{23}^2 + m_{h_3}^2 R_{33}^2 - 2a_1 v_s}{v_s^2}, \\ \lambda_7 &= \frac{m_{h_1}^2 R_{11} R_{13} + m_{h_2}^2 R_{21} R_{23} + m_{h_3}^2 R_{31} R_{33}}{v v_s c_\beta}, \\ \lambda_8 &= \frac{m_{h_1}^2 R_{12} R_{13} + m_{h_2}^2 R_{22} R_{23} + m_{h_3}^2 R_{32} R_{33}}{v v_s s_\beta}, \end{aligned} \quad (13)$$

with shorthand notation $t_\beta \equiv \tan \beta$.

In order to avoid the flavor changing neutral current at the tree-level, one imposes a $\mathbb{Z}'_2$ symmetry (see, e.g., the recent review [135]),

$$u_R \rightarrow -u_R, d_R \rightarrow -d_R, e_R \rightarrow -e_R, \Phi_2 \rightarrow -\Phi_2, \quad (14)$$

while the other fields remain unchanged. This results in the well-known type-I Yukawa interactions,

$$-\mathcal{L} = Y_{u2} \bar{Q}_L \tilde{\Phi}_2 u_R + Y_{d2} \bar{Q}_L \Phi_2 d_R + Y_{e2} \bar{L}_L \Phi_2 e_R + \text{h.c.} \quad (15)$$

Where $Q_L^T = (u_L, d_L)$, $L_L^T = (\nu_L, l_L)$, $\tilde{\Phi}_2 = i\tau_2 \Phi_2^*$, and Y_{u2} ,

Y_{d2} and Y_{e2} are 3×3 matrices in family space. However, the $\mathbb{Z}'_2$ symmetry is explicitly broken in the scalar potential of Eq. (2).

The neutral Higgs boson couplings, normalized to the SM values, are given by

$$\begin{aligned} y_V^{h_1} &= c_2 c_{\beta 1}, y_f^{h_1} = c_2 (c_{\beta 1} - s_{\beta 1} \kappa_f), \\ y_V^{h_2} &= c_3 s_{\beta 1} - s_2 s_3 c_{\beta 1}, \\ y_f^{h_2} &= c_3 (s_{\beta 1} + c_{\beta 1} \kappa_f) - s_2 s_3 (c_{\beta 1} - s_{\beta 1} \kappa_f), \\ y_V^{h_3} &= -s_3 s_{\beta 1} - s_2 c_3 c_{\beta 1}, \\ y_f^{h_3} &= -s_3 (s_{\beta 1} + c_{\beta 1} \kappa_f) - s_2 c_3 (c_{\beta 1} - s_{\beta 1} \kappa_f), \\ y_V^A &= 0, y_f^A = -i\kappa_f \text{ (for } u), y_f^A = i\kappa_f \text{ (for } d, \ell). \end{aligned} \quad (16)$$

Here $\kappa_f = 1/\tan \beta$ and V stands for Z or W . The shorthand notations are defined as $c_{\beta 1} \equiv \cos(\beta - \alpha_1)$ and $s_{\beta 1} \equiv \sin(\beta - \alpha_1)$.

The charged Higgs Yukawa couplings are given by

$$\begin{aligned} \mathcal{L}_Y &= -\frac{\sqrt{2}}{v} H^+ \left\{ \bar{u}_i [\kappa_f (V_{CKM})_{ij} m_{d_j} P_R \right. \\ &\quad \left. - \kappa_f m_{u_i} (V_{CKM})_{ij} P_L] d_j + \kappa_f \bar{\nu} m_\ell P_R \ell \right\} + \text{h.c.}, \end{aligned} \quad (17)$$

where $i, j = 1, 2, 3$ are the index of generation.

III. RELEVANT THEORETICAL AND EXPERIMENTAL CONSTRAINTS

In our discussions, we take into account the following theoretical and experimental constraints:

(1) Vacuum stability. The following conditions are required by the vacuum stability [129],

$$\Omega_1 \text{ or } \Omega_2 \quad (18)$$

with

$$\Omega_1 = \left\{ \lambda_1, \lambda_2, \lambda_6 > 0; \sqrt{\lambda_1 \lambda_6} + \lambda_7 > 0; \sqrt{\lambda_2 \lambda_6} + \lambda_8 > 0; \right.$$

$$\left. \sqrt{\lambda_1 \lambda_2} + \lambda_3 + D > 0; \lambda_7 + \sqrt{\frac{\lambda_1}{\lambda_2}} \lambda_8 \geq 0 \right\},$$

$$\Omega_2 = \left\{ \lambda_1, \lambda_2, \lambda_6 > 0; \sqrt{\lambda_2 \lambda_6} \geq \lambda_8 > -\sqrt{\lambda_2 \lambda_6}; \sqrt{\lambda_1 \lambda_6} > \right.$$

$$\left. -\lambda_7 \geq \sqrt{\frac{\lambda_1}{\lambda_2}} \lambda_8; \right.$$

$$\left. \sqrt{(\lambda_7^2 - \lambda_1 \lambda_6)(\lambda_8^2 - \lambda_2 \lambda_6)} > \lambda_7 \lambda_8 - (D + \lambda_3) \lambda_6 \right\}.$$

(19)

Here $D = \min(\lambda_4 - |\lambda_5|, 0)$.

(2) Tree-level perturbative unitarity. The eigenvalues of the $2 \rightarrow 2$ scalar-scalar scattering matrix are below 8π , which are [129]

$$\begin{aligned} |\lambda_3 - \lambda_4| &< 8\pi \\ |\lambda_3 + 2\lambda_4 \pm 3\lambda_5| &< 8\pi \\ \left| \frac{1}{2} \left(\lambda_1 + \lambda_2 + \sqrt{(\lambda_1 - \lambda_2)^2 + 4\lambda_4^2} \right) \right| &< 8\pi \\ \left| \frac{1}{2} \left(\lambda_1 + \lambda_2 + \sqrt{(\lambda_1 - \lambda_2)^2 + 4\lambda_5^2} \right) \right| &< 8\pi \\ |\lambda_7|, |\lambda_8| &< 8\pi, \\ \frac{1}{2}|a_{1,2,3}| &< 8\pi, \end{aligned} \quad (20)$$

where $a_{1,2,3}$ are the real roots of the cubic equation,

$$\begin{aligned} 0 = & 4 \left(-27\lambda_1\lambda_2\lambda_6 + 12\lambda_3^2\lambda_6 + 12\lambda_3\lambda_4\lambda_6 + 3\lambda_4^2\lambda_6 \right. \\ & + 6\lambda_2\lambda_7^2 - 8\lambda_3\lambda_7\lambda_8 - 4\lambda_4\lambda_7\lambda_8 + 6\lambda_1\lambda_8^2 \\ & + x(36\lambda_1\lambda_2 - 16\lambda_3^2 - 16\lambda_3\lambda_4 - 4\lambda_4^2 + 18\lambda_1\lambda_6 \\ & + 18\lambda_2\lambda_6 - 4\lambda_7^2 - 4\lambda_8^2) \\ & \left. + x^2(-6(\lambda_1 + \lambda_2) - 3\lambda_6) + x^3 \right). \end{aligned} \quad (21)$$

(3) The 125 GeV Higgs signal data. We identify h_2 as the observed 125 GeV Higgs boson and use HiggsTools [136] to compute the total χ_{125}^2 based on the latest LHC measurements of signal strength of the 125 GeV Higgs boson. HiggsTools integrates both HiggsSignals [136,137] and HiggsBounds [138,139]. In particular, we focus on the parameter points that satisfy $\chi_{125}^2 - \chi_{SM}^2 < 6.18$, where χ_{SM}^2 stands for the SM prediction value. These points are preferred over the SM at the 2σ confidence level, assuming a two-parameter fit.

(4) Searches for additional Higgs boson at the collider and flavor observables. We utilize Higgstools to retain only those parameter points that are consistent with the 95% confidence level exclusion limits from collider searches for additional Higgs bosons. We employ SuperIso-v4.1 [140] to assess the bound of $B \rightarrow X_s \gamma$ decay.

(5) The oblique parameters. The oblique parameters provide important constraints on the Higgs mass spectrum within the model. To ensure consistency with experimental data, parameter points are required to lie within the 2σ confidence region for both the S and T parameters. This corresponds to $\chi^2 < 6.18$ for two degrees of freedom. The corresponding fit results can be found in Ref. [141],

$$S = 0.00 \pm 0.07, \quad T = 0.05 \pm 0.06, \quad (22)$$

with a correlation coefficient $\rho_{ST} = 0.92$.

In the model, the approximate calculations of the S and T parameters are [142,143]

$$\begin{aligned} S = & \frac{1}{\pi m_Z^2} \left[\sum_{i=1,2,3} (F_S(m_Z^2, m_{h_i}^2, m_A^2)(-s_\beta R_{i1} + c_\beta R_{i2})^2 \right. \\ & + F_S(m_Z^2, m_Z^2, m_{h_i}^2)(c_\beta R_{i1} + s_\beta R_{i2})^2 \\ & - m_Z^2 F_{S0}(m_Z^2, m_Z^2, m_{h_i}^2)(c_\beta R_{i1} + s_\beta R_{i2})^2 \\ & - F_S(m_Z^2, m_{H^\pm}^2, m_{H^\pm}^2) - F_S(m_Z^2, m_Z^2, m_{ref}^2) \\ & \left. + m_Z^2 F_{S0}(m_Z^2, m_Z^2, m_{ref}^2) \right], \\ T = & \frac{1}{16\pi m_W^2 s_W^2} \left[\sum_{i=1,2,3} (-F_T(m_{h_i}^2, m_A^2)(-s_\beta R_{i1} + c_\beta R_{i2})^2 \right. \\ & + F_T(m_{H^\pm}^2, m_{h_i}^2)(c_\beta R_{i2} - s_\beta R_{i1})^2 \\ & + 3F_T(m_Z^2, m_{h_i}^2)(c_\beta R_{i1} + s_\beta R_{i2})^2 \\ & - 3F_T(m_W^2, m_{h_i}^2)(c_\beta R_{i1} + s_\beta R_{i2})^2 \\ & \left. + F_T(m_{H^\pm}^2, m_A^2) - 3F_T(m_Z^2, m_{ref}^2) + 3F_T(m_W^2, m_{ref}^2) \right], \end{aligned} \quad (23)$$

with

$$\begin{aligned} F_T(a, b) &= \frac{1}{2}(a + b) - \frac{ab}{a - b} \log\left(\frac{a}{b}\right), \\ F_S(a, b, c) &= B_{22}(a, b, c) - B_{22}(0, b, c), \\ F_{S0}(a, b, c) &= B_0(a, b, c) - B_0(0, b, c) \end{aligned} \quad (24)$$

where

$$\begin{aligned} B_{22}(a, b, c) &= \frac{1}{4} \left[b + c - \frac{1}{3}a \right] - \frac{1}{2} \int_0^1 dx X \log(X - i\epsilon), \\ B_0(a, b, c) &= - \int_0^1 dx \log(X - i\epsilon), \\ X &= bx + c(1 - x) - ax(1 - x). \end{aligned} \quad (25)$$

IV. THE DIPHOTON AND $b\bar{b}$ EXCESSES AT 95.4 GEV

The combined analysis of ATLAS and CMS diphoton data at 95.4 GeV reveals a 3.1σ local excess [4].

$$\mu_{\gamma\gamma}^{exp} = \mu_{\gamma\gamma}^{ATLAS+CMS} = 0.24_{-0.08}^{+0.09}. \quad (26)$$

Intriguingly, a persistent local excess with a significance of 2.3σ was also observed in the $e^+e^- \rightarrow Z(\phi \rightarrow b\bar{b})$ channel at LEP in the same mass region [1],

$$\mu_{b\bar{b}}^{exp} = 0.117 \pm 0.057. \quad (27)$$

The observed excesses in the diphoton and $b\bar{b}$ channels at 95.4 GeV are attributed to resonant production of the lightest CP-even Higgs boson, h_1 . Under the narrow width approximation, the corresponding signal strengths can be formulated as follows:

$$\begin{aligned} \mu_{b\bar{b}} &= \frac{\sigma_{\text{N2HDM}}(e^+e^- \rightarrow Zh_1)}{\sigma_{\text{SM}}(e^+e^- \rightarrow Zh_{95.4}^{\text{SM}})} \times \frac{\text{BR}_{\text{N2HDM}}(h_1 \rightarrow b\bar{b})}{\text{BR}_{\text{SM}}(h_{95.4}^{\text{SM}} \rightarrow b\bar{b})} \\ &= |y_V^{h_1}|^2 \frac{\text{BR}_{\text{N2HDM}}(h_1 \rightarrow b\bar{b})}{\text{BR}_{\text{SM}}(h_{95.4}^{\text{SM}} \rightarrow b\bar{b})}, \end{aligned} \quad (28)$$

$$\begin{aligned} \mu_{\gamma\gamma} &= \frac{\sigma_{\text{N2HDM}}(gg \rightarrow h_1)}{\sigma_{\text{SM}}(gg \rightarrow h_{95.4}^{\text{SM}})} \times \frac{\text{BR}_{\text{N2HDM}}(h_1 \rightarrow \gamma\gamma)}{\text{BR}_{\text{SM}}(h_{95.4}^{\text{SM}} \rightarrow \gamma\gamma)} \\ &\simeq |y_f^{h_1}|^2 \frac{\text{BR}_{\text{N2HDM}}(h_1 \rightarrow \gamma\gamma)}{\text{BR}_{\text{SM}}(h_{95.4}^{\text{SM}} \rightarrow \gamma\gamma)}. \end{aligned} \quad (29)$$

To assess the capability to simultaneously account for the observed excesses in the $\gamma\gamma$ and $b\bar{b}$ channels, we conduct a χ_{95}^2 analysis,

$$\chi_{95}^2 = \frac{(\mu_{\gamma\gamma} - 0.24)^2}{0.085^2} + \frac{(\mu_{b\bar{b}} - 0.117)^2}{0.057^2}, \quad (30)$$

and explain the diphoton and $b\bar{b}$ excesses within the 2σ ranges, namely $\chi_{95}^2 < 6.18$.

In the model, the decay $h_1 \rightarrow \gamma\gamma$ is induced at the one-loop level, whose width is calculated as

$$\begin{aligned} \Gamma(h_1 \rightarrow \gamma\gamma) &= \frac{\alpha^2 m_{h_1}^3}{256\pi^3 v^2} \left| y_V^{h_1} F_1(\tau_{W^\pm}) + y_{H^\pm} F_0(\tau_{H^\pm}) \right. \\ &\quad \left. + \sum_f y_f^{h_1} N_{cf} Q_f^2 F_{1/2}(\tau_f) \right|^2, \end{aligned} \quad (31)$$

where $\tau_i = \frac{4m_i^2}{m_{h_1}^2}$, and N_{cf} and Q_f are electric charge and the number of color degrees of freedom of the fermion in the loop. The factor $y_{H^\pm}$ is

$$y_{H^\pm} = \frac{v}{2m_{h^\pm}^2} g_{h_1 H^+ H^-} \quad (32)$$

with

$$\begin{aligned} g_{h_1 H^+ H^-} &= \frac{1}{v} \left(-\frac{m_{12}^2}{s_\beta c_\beta} \left[\frac{R_{11}}{c_\beta} + \frac{R_{12}}{s_\beta} \right] + m_{h_1}^2 \left[\frac{R_{11} s_\beta^2}{c_\beta} + \frac{R_{12} c_\beta^2}{s_\beta} \right] \right. \\ &\quad \left. + 2m_{H^\pm}^2 [R_{11} c_\beta + R_{12} s_\beta] \right) \end{aligned} \quad (33)$$

The functions $F_{1,0,1/2}$ are defined as [144]

$$\begin{aligned} F_1(\tau) &= 2 + 3\tau + 3\tau(2 - \tau)f(\tau), \\ F_{1/2}(\tau) &= -2\tau[1 + (1 - \tau)f(\tau)], \\ F_0(\tau) &= \tau[1 - \tau f(\tau)], \end{aligned} \quad (34)$$

with

$$f(\tau) = \begin{cases} [\sin^{-1}(1/\sqrt{\tau})]^2, & \tau \geq 1 \\ -\frac{1}{4}[\ln(\eta_+/ \eta_-) - i\pi]^2, & \tau < 1 \end{cases} \quad (35)$$

where $\eta_\pm = 1 \pm \sqrt{1 - \tau}$.

In our calculations, we take two different scenarios:

Scenario A: By choosing a small value of c_2 , the 95.4 GeV Higgs boson (h_1) is predominantly singlet-like, originating mainly from the singlet field Φ_S . Under the approximation of $s_2 \simeq \text{sgn}(s_2)(1 - \frac{c_2^2}{2})$, the couplings h_2 and h_3 normalized to the SM are given by

$$\begin{aligned} y_V^{h_2} &\simeq |s_2| s_{\beta 13} + \frac{c_2^2}{2} c_3 s_{\beta 1}, \quad y_f^{h_2} \simeq |s_2| (s_{\beta 13} + c_{\beta 13} \kappa_f) \\ &\quad + \frac{c_2^2}{2} c_3 (s_{\beta 1} + c_{\beta 1} \kappa_f), \\ y_V^{h_3} &\simeq |s_2| c_{\beta 13} - \frac{c_2^2}{2} c_3 s_{\beta 1}, \quad y_f^{h_3} \simeq |s_2| (c_{\beta 13} - s_{\beta 13} \kappa_f) \\ &\quad - \frac{c_2^2}{2} c_3 (s_{\beta 1} + c_{\beta 1} \kappa_f), \end{aligned} \quad (36)$$

where $c_{\beta 13} \equiv \cos(\beta - \alpha_1 - \text{sgn}(s_2)\alpha_3)$ and $s_{\beta 13} \equiv \sin(\beta - \alpha_1 - \text{sgn}(s_2)\alpha_3)$. The mixing parameters are chosen as follows:

$$0 \leq c_2 \leq 0.4, \quad s_{\beta 13} = 1.0, \quad 0 \leq c_{\beta 1} \leq 1.0, \quad 1 \leq \tan\beta \leq 15. \quad (37)$$

When $s_{\beta 13} = 1.0$ and c_2 approaches zero, the couplings of h_2 to the SM particles converge to those of the SM Higgs boson, which is favored by the observed signal data for the 125 GeV Higgs.

Scenario B: The mixing parameters are scanned over the following ranges:

$$0 \leq c_{\beta 1} \leq 0.4, \quad -0.4 \leq s_3 \leq 0.4, \quad 0 \leq c_2 \leq 1, \quad 1 \leq \tan\beta \leq 15. \quad (38)$$

In the limits of $c_{\beta 1} \rightarrow 0$ and $|s_3| \rightarrow 0$, the couplings of h_2 to the SM particles approach those of the SM, which is favored by the signal measurements of the 125 GeV Higgs. In addition, when $c_2 \rightarrow 1$, the 95.4 GeV Higgs boson (h_1) predominantly originates from the mixing of the

two CP-even components of the Higgs doublets.

After imposing the relevant theoretical constraints, the oblique parameters, the Higgs signal data at 125 GeV, searches for additional Higgs bosons at the collider, and flavor observables, we identify the parameter space in scenario A that accounts for the observed excesses in the $b\bar{b}$ and diphoton channels at 95.4 GeV in Fig. 1. As indicated by Eq. (36), within the selected parameter space of scenario A, the coupling of h_2 to vector bosons, $y_V^{h_2}$, tends to be smaller than its coupling to fermions, $y_f^{h_2}$, as illustrated in the left panel. The Higgs signal data at 125 GeV impose a lower bound on $y_V^{h_2}$, requiring $y_V^{h_2} > 0.93$. In the parameter space consistent with the 125 GeV Higgs measurements, collider limits on additional Higgs bosons, and constraints from flavor physics, the coupling $y_V^{h_1}$ is restricted to values below 0.38. Furthermore, the condition $\chi_{95}^2 < 6.18$ is satisfied in the region of $0.2 \leq y_V^{h_1} \leq 0.38$, with $y_f^{h_1}$ bounded from below. In addition, the Higgs sig-

nal data at 125 GeV exclude a small corner of the parameter space characterized by $c_{\beta 1} \rightarrow 1$ and $c_2 \rightarrow 0.4$. In such region both $y_V^{h_2}$ and $y_f^{h_2}$ can exhibit significant deviations from unity.

As shown in the left panel of Fig. 2, the value of χ_{95}^2 is sensitive to $y_V^{h_1}$ and $y_f^{h_1}$, and decreases as they increase. The condition $\chi_{95}^2 < 2.3$ is satisfied in partial region of parameter space, with the minimum value attaining 1.2, which indicates that the model can explain the diphoton and $b\bar{b}$ excesses within the 1σ ranges. The signal strength $\mu_{b\bar{b}}$ is proportional to $|y_V^{h_1}|^2$. Meanwhile, the W -loop can play an important contribution to the width of $h_1 \rightarrow \gamma\gamma$, and therefore the signal strength $\mu_{\gamma\gamma}$ is also affected by $y_V^{h_1}$. The interpretation of the $b\bar{b}$ excess imposes a lower bound on $|y_f^{h_1}|$. Because of $y_V^{h_1} = c_2 c_{\beta 1}$, the value of χ_{95}^2 tends to decrease as c_2 and $c_{\beta 1}$ increase, as shown in the middle panel of Fig. 2. When $c_{\beta 1}$ or $\tan\beta$ is large, the $y_f^{h_1}$ will has a mild dependence on $\tan\beta$ (See Eq. (16)). From

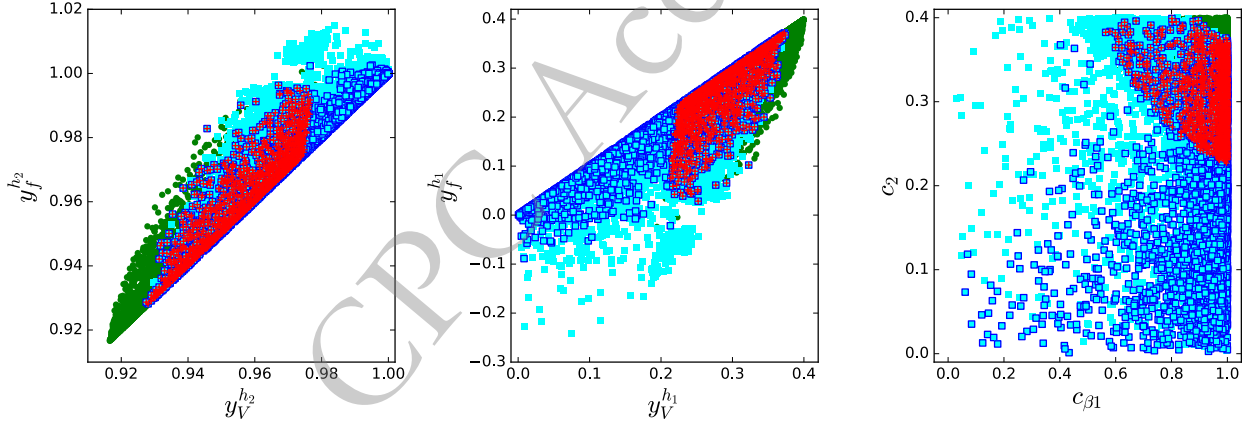


Fig. 1. (color online) In scenario A, the parameter space is progressively constrained by sequentially imposing the following: theoretical requirements and the oblique parameters; the signal data of the 125 GeV Higgs boson; searches for additional Higgs bosons at the collider and flavor observables; and finally the condition $\chi_{95}^2 < 6.18$. The surviving parameter points at each stage are represented by green bullets, cyan squares, blue-edged squares, and red pluses, respectively.

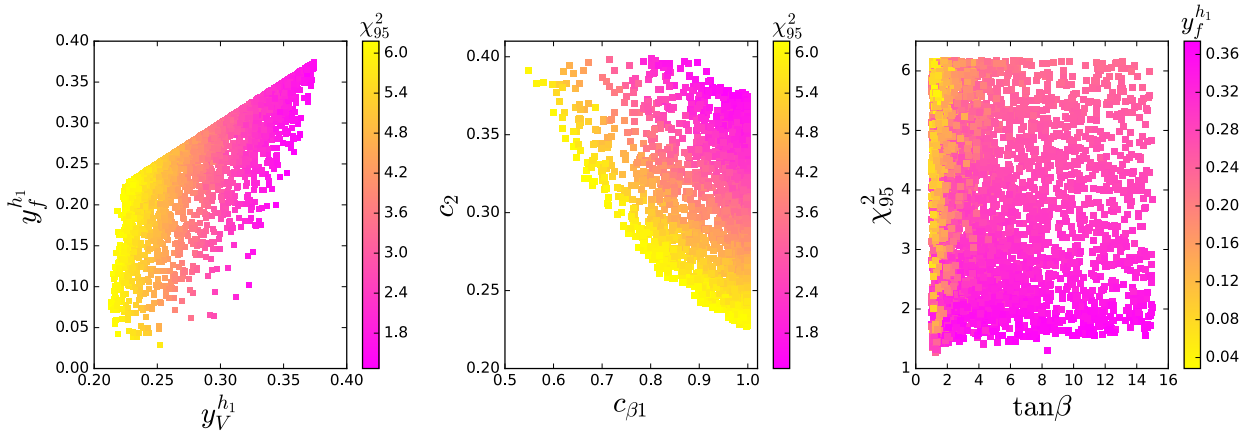


Fig. 2. (color online) In scenario A, the surviving parameter points satisfy $\chi_{95}^2 < 6.18$ and simultaneously meet the theoretical constraints, the oblique parameters, the Higgs signal data at 125 GeV, searches for additional Higgs bosons at the collider, and flavor observables.

the right panel of Fig. 2, it is observed that the value of χ_{95}^2 shows limited sensitivity to $\tan\beta$.

Similar to Fig. 1, we display the parameter points for scenario B that accounts for the observed excesses in the $b\bar{b}$ and diphoton channels at 95.4 GeV in Fig. 3. Unlike scenario A, the allowed region in scenario B includes not only the positive $y_f^{h_1}$ region but also a narrow band where $y_f^{h_1}$ takes negative values. The signal data of the 125 GeV Higgs boson requires a small $c_{\beta 1}$, allowing for a negative $y_f^{h_1}$, see Eq. (16). The condition $\chi_{95}^2 < 6.18$ is satisfied in the region of $0.18 < c_{\beta 1} < 0.35$ and $0.88 < c_2 < 1$. For such large c_2 , the 95.4 GeV Higgs boson mainly originates from the mixing of the two CP-even components of the Higgs doublets.

As in scenario A, the value of χ_{95}^2 in scenario B decreases as $y_V^{h_1}$ and $|y_f^{h_1}|$ (c_2 and $c_{\beta 1}$) increase, as illustrated in the upper-left panel and upper-right panel of Fig. 4. However, different from scenario A, the minimal value of χ_{95}^2 in scenario B only reaches to 2, suggesting that the model can only marginally explain the diphoton and $b\bar{b}$ excesses at the 1σ level. Furthermore, the condition $\chi_{95}^2 < 6.18$ disfavors a narrow region around $\tan\beta \sim 4$, where the value of $|y_f^{h_1}|$ is significantly suppressed. The parameter s_3 is favored to vary from -0.3 to 0.25, and is not sensitive to c_2 . Its absolute value decreases with increasing $c_{\beta 1}$ in order to maintain a sufficiently large $y_V^{h_2}$ to accommodate the signal data of the 125 GeV Higgs boson.

V. DOMAIN WALLS AND GRAVITATIONAL WAVES

The classical scalar fields are parameterized as

$$\Phi_1 = \begin{pmatrix} 0 \\ \frac{\phi_1(z)}{\sqrt{2}} \end{pmatrix}, \quad \Phi_2 = \begin{pmatrix} 0 \\ \frac{\phi_2(z)}{\sqrt{2}} \end{pmatrix}, \quad \Phi_S = \phi_S(z), \quad (39)$$

where z is a coordinate perpendicular to domain walls [145]. The expression for the energy density of the domain walls is given by

$$\varepsilon_{\text{wall}} = \frac{1}{2}(\partial_z \phi_1)^2 + \frac{1}{2}(\partial_z \phi_2)^2 + \frac{1}{2}(\partial_z \phi_S)^2 + V(\phi_1, \phi_2, \phi_S) - V(v_1, v_2, v_s), \quad (40)$$

with the scalar potential

$$\begin{aligned} V(\phi_1, \phi_2, \phi_S) = & \frac{m_{11}^2}{2} \phi_1^2 + \frac{\lambda_1}{8} \phi_1^4 + \frac{m_{22}^2}{2} \phi_2^2 \\ & + \frac{\lambda_2}{8} \phi_2^4 - m_{12}^2 \phi_1 \phi_2 + \frac{\lambda_{345}}{4} \phi_1^2 \phi_2^2 \\ & + \frac{m_S^2}{2} \phi_S^2 + \frac{\lambda_6}{8} \phi_S^4 + \frac{\lambda_7}{4} \phi_1^2 \phi_S^2 \\ & + \frac{\lambda_8}{4} \phi_2^2 \phi_S^2 - a_1 v_s^2 \phi_S + \frac{a_1}{3} \phi_S^3. \end{aligned} \quad (41)$$

The equations of motion for domain walls are

$$\frac{d^2 \phi_i}{dz^2} = \frac{\partial V(\phi_1, \phi_2, \phi_S)}{\partial \phi_i}, \quad (\phi_i = \phi_1, \phi_2, \phi_S), \quad (42)$$

with the boundary conditions

$$\lim_{z \rightarrow \pm\infty} \phi_1(z) = v_1, \quad \lim_{z \rightarrow \pm\infty} \phi_2(z) = v_2, \quad \lim_{z \rightarrow \pm\infty} \phi_S(z) = \pm v_s. \quad (43)$$

We modify CosmoTransitions [146] to approximately solve Eqs. (42) and (43), and relevant computational details are provided in [146,147]. The domain wall tension σ_{wall} is computed through an integration of the energy density $\varepsilon_{\text{wall}}$ over the z axis,

$$\sigma_{\text{wall}} = \int dz \varepsilon_{\text{wall}}. \quad (44)$$

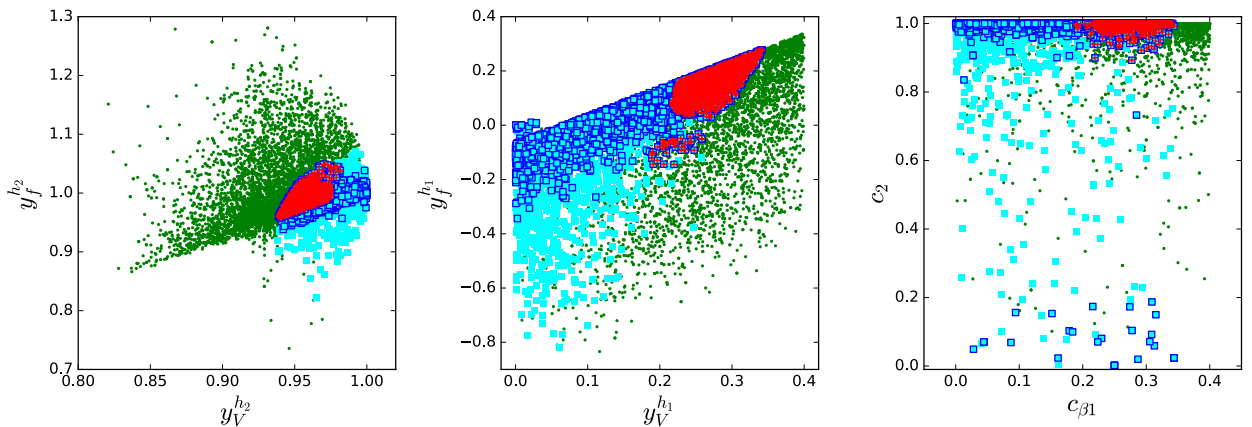


Fig. 3. (color online) Same as the Fig. 1, but for scenario B.

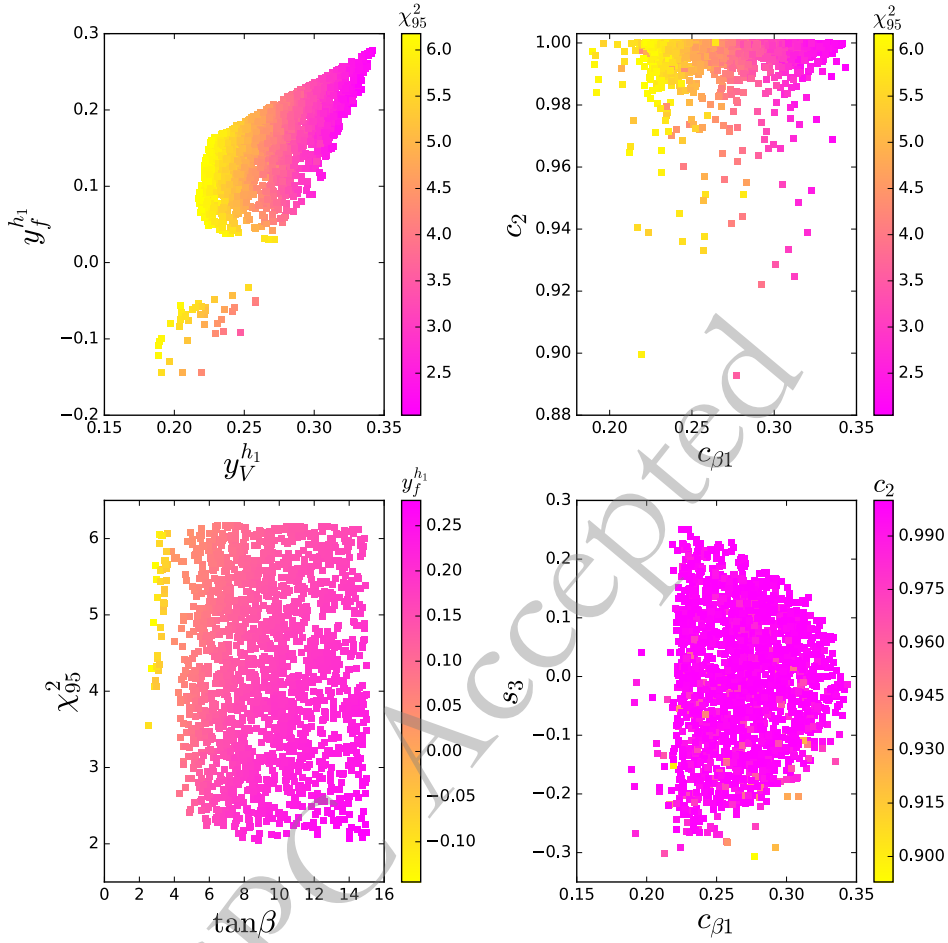


Fig. 4. (color online) Same as the Fig. 2, but for scenario B.

Domain walls must collapse before they can over-close the Universe. The volume pressure induced by energy bias (V_{bias}) exerts a force on the domain walls, and drives the contraction of regions occupied by the false vacuum. The collapse of domain wall occurs when the volume pressure force becomes comparable to the tension force. The characteristic temperature at which the domain walls annihilate can be estimated by [148,149]

$$T_{\text{ann}} = 3.41 \times 10^{-2} \text{ GeV } C_{\text{ann}}^{-1/2} A^{-1/2} \left(\frac{g_*(T_{\text{ann}})}{10} \right)^{-1/4} \hat{\sigma}_{\text{wall}}^{-1/2} \hat{V}_{\text{bias}}^{1/2}, \quad (45)$$

with

$$\hat{\sigma}_{\text{wall}} \equiv \frac{\sigma_{\text{wall}}}{\text{TeV}^3}, \quad \hat{V}_{\text{bias}} \equiv \frac{V_{\text{bias}}}{\text{MeV}^4}. \quad (46)$$

In this analysis, we adopt a constant $C_{\text{ann}} = 5$ [149] and set the area parameter $A \approx 0.8$ for the Z_2 symmetric model [148]. The energetic particles released from the collapse of domain walls have the potential to disrupt the synthesis of light nuclei formed during Big Bang Nucle-

osynthesis (BBN) [150]. To preserve the successful predictions of BBN, it is therefore imperative that the domain walls annihilate before the BBN epoch, $T_{\text{ann}} > T_{\text{BBN}} = 8.6 \times 10^{-3} \text{ GeV}$. In addition, in order to ensure that domain walls annihilate before their energy density dominates the Universe, a lower bound must be imposed on V_{bias} [149]

$$V_{\text{bias}}^{1/4} > 2.18 \times 10^{-5} \quad C_{\text{ann}}^{1/4} \quad A^{1/2} \hat{\sigma}_{\text{wall}}^{1/2}. \quad (47)$$

Following the annihilation of domain walls, a SGWB is produced, and the peak frequency is given by [148]

$$\begin{aligned} f_{\text{peak}} &\simeq 1.1 \times 10^{-7} \text{ Hz} \left(\frac{g_*(T_{\text{ann}})}{10} \right)^{1/2} \left(\frac{g_{*s}(T_{\text{ann}})}{10} \right)^{-1/3} \left(\frac{T_{\text{ann}}}{1 \text{ GeV}} \right) \\ &\simeq 3.75 \times 10^{-9} \text{ Hz} \left(\frac{g_*(T_{\text{ann}})}{10} \right)^{1/4} \left(\frac{g_{*s}(T_{\text{ann}})}{10} \right)^{-1/3} \\ &\quad \times C_{\text{ann}}^{-1/2} A^{-1/2} \hat{\sigma}_{\text{wall}}^{-1/2} \hat{V}_{\text{bias}}^{1/2}. \end{aligned} \quad (48)$$

Here, $g_*(T_{\text{ann}})$ and $g_{*s}(T_{\text{ann}})$ count the relativistic degrees

of freedom contributing to the energy density and the entropy density. Within the temperature range $1\text{ MeV} \lesssim T_{\text{ann}} \lesssim 100\text{ MeV}$, both quantities take the value 10.75 [151].

The peak amplitude of the GW spectrum at the present time is [148,149]

$$\Omega_{\text{GW}}^{\text{peak}} h^2 = 5.3 \times 10^{-20} \tilde{\epsilon}_{\text{GW}} A^4 C_{\text{ann}}^2 \left(\frac{g_{*s}(T_{\text{ann}})}{10} \right)^{-4/3} \times \left(\frac{g_{*s}(T_{\text{ann}})}{10} \right) \hat{\sigma}_{\text{wall}}^4 \hat{V}_{\text{bias}}^{-2}. \quad (49)$$

with $\tilde{\epsilon}_{\text{GW}} \simeq 0.7 \pm 0.4$ [148]. Given an arbitrary frequency f , we use [148,152]

$$\Omega_{\text{GW}} h^2(f < f_{\text{peak}}) = \Omega_{\text{GW}}^{\text{peak}} h^2 \left(\frac{f}{f_{\text{peak}}} \right)^3, \quad (50)$$

$$\Omega_{\text{GW}} h^2(f > f_{\text{peak}}) = \Omega_{\text{GW}}^{\text{peak}} h^2 \left(\frac{f_{\text{peak}}}{f} \right). \quad (51)$$

In our discussions, we take $10^{-9}\text{ Hz} \leq f_{\text{peak}} \leq 10^{-7}\text{ Hz}$,

and get T_{ann} from the first line of Eq. (48). $\hat{V}_{\text{bias}}$ is obtained from the second line of Eq. (48) with f_{peak} and $\hat{\sigma}_{\text{wall}}$ calculated in the parameter points accommodating the diphoton and $b\bar{b}$ excesses at 95.4 GeV. In Fig. 5 and Fig. 6, we display the parameter points that satisfy $\chi_{95}^2 < 6.18$ and $\Omega_{\text{GW}}^{\text{peak}} h^2 > 10^{-15}$ for $f_{\text{peak}} = 10^{-9}\text{ Hz}$ while remaining consistent with relevant theoretical and experimental constraints mentioned above, for scenario A and scenario B, respectively.

The peak amplitude $\Omega_{\text{GW}}^{\text{peak}}$ increases with decreasing f_{peak} and increasing $\hat{\sigma}_{\text{wall}}$, as indicated by the second line of Eq. (48) and Eq. (49), and as illustrated in the upper-left and upper-right panels of Fig. 5. In scenario A, although the 95.4 GeV Higgs boson (h_1) predominantly originates from the real singlet field, it must include non-negligible components of the Higgs doublets to acquire the necessary couplings to gauge bosons and fermions, thereby accounting for the observed diphoton and $b\bar{b}$ excesses at 95.4 GeV. Thus, both R_{31} and R_{32} can not approach to zero, theoretical constraints on $\lambda_{1,2,3}$ will impose a lower bound on m_{h_3} , $m_{h_3} < 1.5\text{ TeV}$ (see the first three lines of Eq. (13)). As a result, according to the sixth

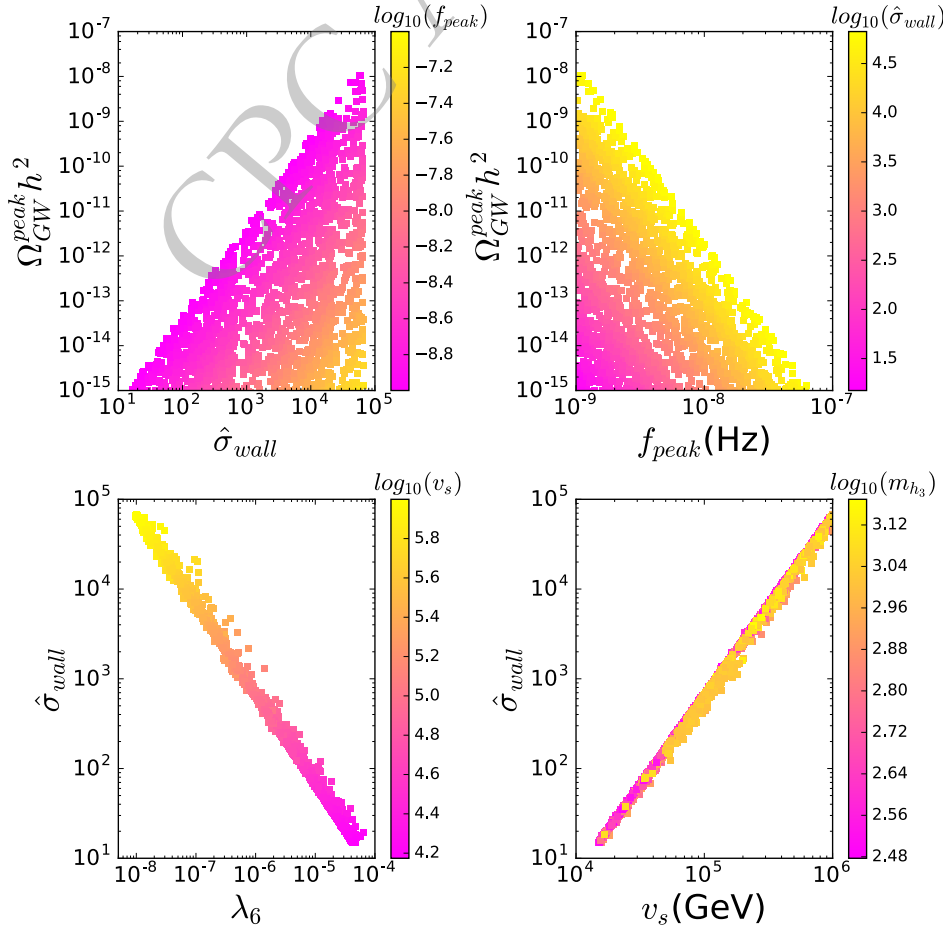


Fig. 5. (color online) In scenario A, the parameter points satisfy $\Omega_{\text{GW}}^{\text{peak}} h^2 > 10^{-15}$ and $\chi_{95}^2 < 6.18$, while also complying with the theoretical and experimental constraints discussed above.

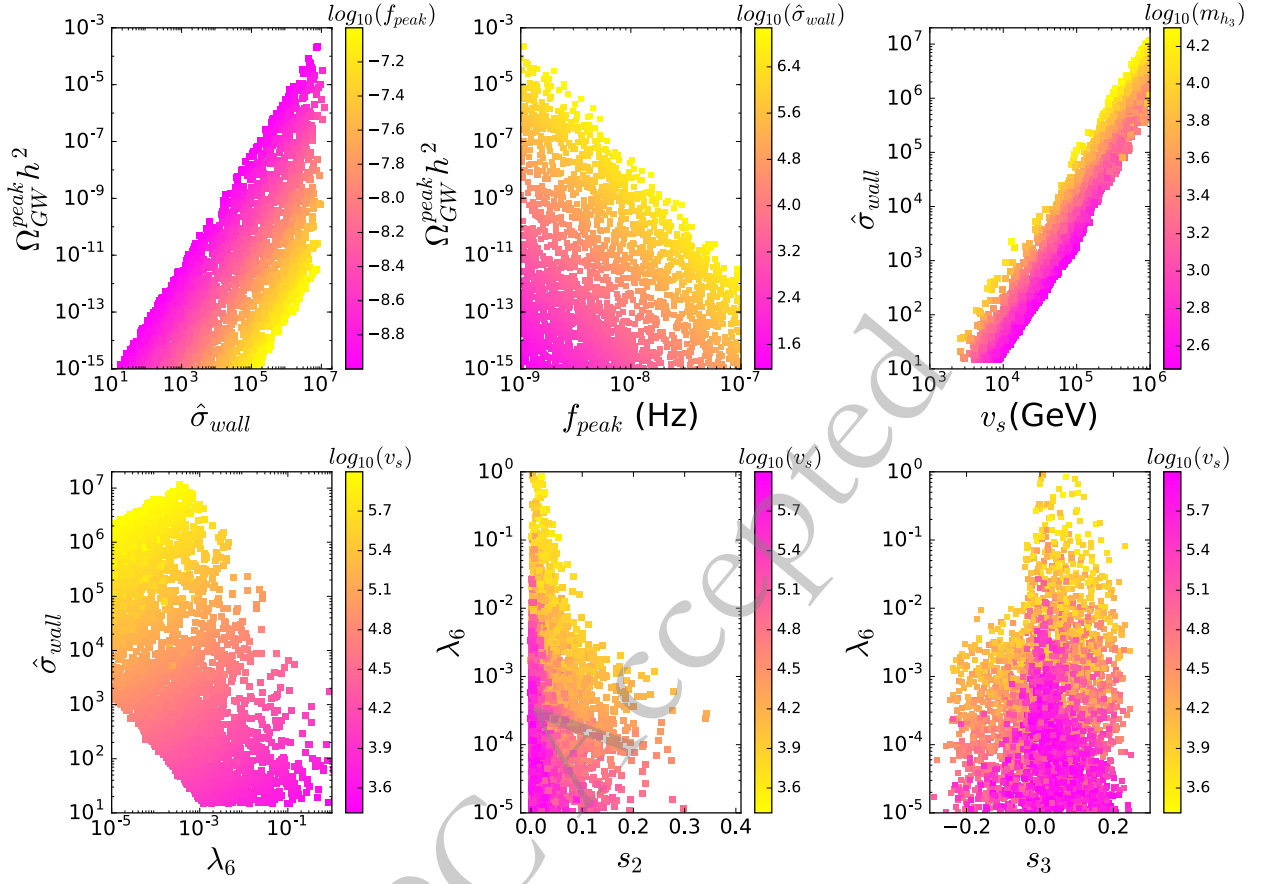


Fig. 6. (color online) Same as the Fig. 5, but for scenario B.

line of Eq. (13), λ_6 decreases with increasing v_s , yielding a range of $10^{-8} < \lambda_6 < 10^{-4}$ for $14 \text{ TeV} < v_s < 1000 \text{ TeV}$. Although λ_6 decreases as v_s increases, the domain wall tension $\hat{\sigma}_{\text{wall}}$ still grows rapidly.

In scenario B, the 95.4 GeV Higgs boson predominantly originates from the CP-even components of the Higgs doublets. Even though the mixing between the singlet and doublet components vanishes (i.e., $R_{31} \rightarrow 0$ and $R_{32} \rightarrow 0$), the 95.4 GeV Higgs boson still can interact with gauge bosons and fermions to explain the diphoton and $b\bar{b}$ excesses at 95.4 GeV. Therefore, theoretical constraints on $\lambda_{1,2,3}$ allow m_{h_3} to have a large value, reaching up to 20 TeV for sufficiently small s_2 and s_3 . Consequently, λ_6 is sensitive to s_2 , s_3 , and v_s , and can attain larger value as s_2 , s_3 , and v_s decrease, as illustrated in the lower-middle and lower-right panels of Fig. 6. Since the domain wall tension $\hat{\sigma}_{\text{wall}}$ mainly depends on v_s and λ_6 , as shown in the lower-left panel of Fig. 6, the value of $\hat{\sigma}_{\text{wall}}$ in scenario B can be much larger than that in scenario A, thereby significantly enhancing $\Omega_{\text{GW}}^{\text{peak}}$.

We pick out four benchmark points: BPA1 and BPA2 for scenario A, and BPB1 and BPB2 for scenario B, and display the key input parameters and results in Table 1. We take BPA2 as an example, and show the domain wall profiles of ϕ_1 , ϕ_2 , and ϕ_s for the BPA2 in Fig. 7. From

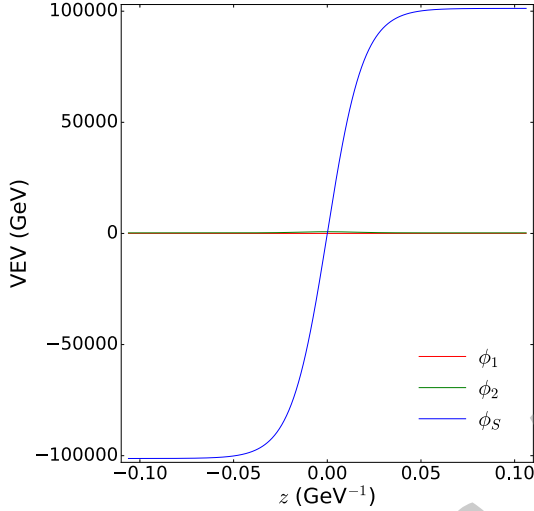
Fig. 7, one can deduce that the domain wall tension σ_{wall} is predominantly determined by the singlet field $\phi_s(z)$ when v_s is very large.

We examine the GW spectra for the four benchmark points, which are shown along with the result of the NANOGrav dataset and the sensitivity curve of SKA in Fig. 8. For the BPB1 with $v_s \approx 980 \text{ TeV}$, the predicted GW spectrum can account for the entire frequency range of the NANOGrav data, from low to high frequencies. For the BPB2 with $v_s = 730 \text{ TeV}$, the predicted GW spectrum explains the NANOGrav data in the low frequency region ($f < 4 \times 10^{-8} \text{ Hz}$) but fails to extend into the higher frequency range. From the parameter points shown in Fig. 5, we select the one with the largest domain wall tension as BPA1. However, the peak amplitude of its GW spectrum only fits the edges of several low-frequency regions of the NANOGrav data. As illustrated in Fig. 8, the GW spectra corresponding to BPA1 and BPA2 exceed the SKA sensitivity curve in several low frequency regions.

We perform a Bayesian analysis of our model using PTArcade [154] and the NANOGrav 15 year data. We employ the Ceffyl mode [155] to derive the posterior distributions of the model parameters. The Enterprise mode [156] is used to evaluate the Bayes factor of our model

Table 1. Input parameters and results for the BPA1, BPA2, BPB1 and BPB2. Here $m_{h_1} = 95.4$ GeV and $m_{h_2} = 125.5$ GeV are fixed.

	m_{h_3} (GeV)	m_A (GeV)	$m_{H^\pm}$ (GeV)	m_{12}^2 (GeV) ²	$\tan\beta$	s_1	s_2	s_3	v_s (GeV)	λ_6	$\hat{\sigma}_{\text{wall}}$	f_{peak}	$\Omega_{\text{GW}}^{\text{peak}} h^2$	χ_{95}^2
BPA1	912.25	887.14	912.25	208668.96	3.51	0.9569	0.9362	-0.9998	999021	1.01×10^{-8}	6.69×10^4	7.0×10^{-9}	2.00×10^{-8}	1.89
BPA2	312.53	465.11	465.11	15778.26	5.13	0.8331	0.9580	-0.9235	101267	1.05×10^{-6}	7.10×10^2	1.5×10^{-9}	2.26×10^{-12}	4.61
BPB1	18418.07	414.86	414.86	553.96	12.53	0.1575	0.0046	0.0350	982846	3.51×10^{-4}	1.19×10^7	1.1×10^{-8}	7.22×10^{-8}	5.77
BPB2	13474.82	476.88	476.88	1161.65	5.30	0.1081	0.0047	0.0313	728781	3.42×10^{-4}	4.78×10^6	1.4×10^{-8}	1.03×10^{-8}	3.01

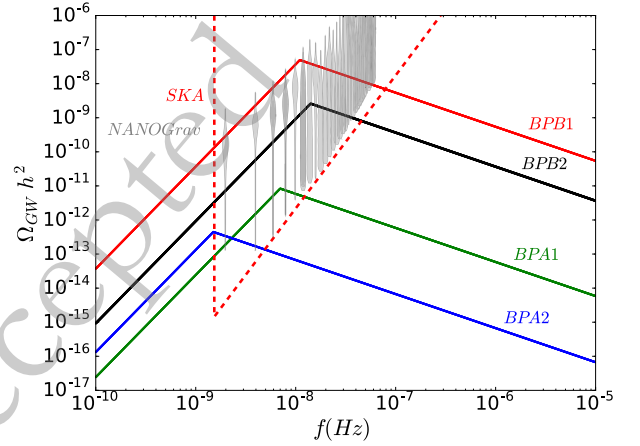
**Fig. 7.** (color online) The domain wall profiles of ϕ_1 , ϕ_2 , and ϕ_S for the BPA2.

relative to the supermassive black hole binaries (SMBHB). The GW background signal from SMBHB is modeled as a power law of the form,

$$\Omega_{\text{GW}}(f)h^2 = \frac{2\pi^2 A_{\text{BHB}}^2}{3H_0} \left(\frac{f}{f_{\text{yr}}}\right)^{5-\gamma_{\text{BHB}}} f_{\text{yr}}^2, \quad (52)$$

wheres $f_{\text{yr}} = \text{year}^{-1} = 3.17 \times 10^{-8}$ Hz and H_0 is the present-day value of the Hubble rate. We adopt a two-dimensional Gaussian prior for γ_{BHB} and A_{BHB} , derived from a power-law fit to the simulated SMBHB populations [69], as implemented in PTArcade.

In Table 2, we provide the priors for parameters of scenario B in our model and the Bayes factor. For very large v_s in the range of 500 TeV and 1000 TeV, the domain wall tension σ_{wall} is almost entirely determined by λ_6 , while being insensitive to other parameters. Consequently, we fix all parameters except v_s and λ_6 for simplicity. We assume that the singlet scalar field exhibits mild mixings with the two Higgs doublets, leading to non-zero values of s_2 and s_3 . As a result, the couplings of the 125 GeV Higgs boson deviate slightly from the SM predictions, which might be tested at the future CEPC. A detailed study of this aspect will be performed in future work. For the chosen values of s_2 and s_3 , as well as $v_s \sim 1000$ TeV, theoretical constraints require

**Fig. 8.** (color online) The GW spectra $\Omega_{\text{GW}} h^2$ as a function of the frequency f . The result of the NANOGrav dataset [63,64] and the sensitivity of SKA [153] are also displayed.

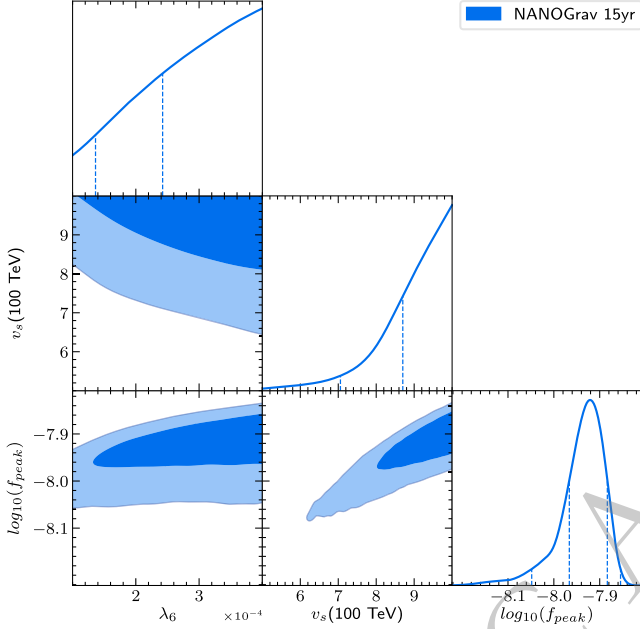
$\lambda_6 < 0.0004$. Simultaneously, we impose that the diphoton and $b\bar{b}$ excesses at 95.4 GeV are accommodated within the 2σ ranges. The Bayes factor is estimated to be approximately 22. The posterior distributions of parameters are shown in Fig. 9. The maximum posterior value of f_{peak} is 1.2×10^{-8} Hz, while $\lambda_6 < 2.4 \times 10^{-4}$ and $v_s < 870$ TeV respectively lie outside the 68% credible interval. For scenario A, even within the optimistic prior ranges, the Bayes factor is found to be nearly zero, consistent with the results shown in Fig. 8.

VI. CONCLUSION

After imposing relevant theoretical and experimental constraints, we studied the diphoton and $b\bar{b}$ excesses at 95.4 GeV, along with the nano-Hertz GW signatures originating from domain walls, within the framework of the N2HDM. We consider two scenarios: in scenario A, the 95.4 GeV Higgs boson is primarily singlet-like, whereas in scenario B, it mainly originates from the CP-even components of the Higgs doublets. We find that scenario A is able to fully reproduce both the diphoton and $b\bar{b}$ excesses at 95.4 GeV within the 1σ range. However, in the parameter space that accommodates both excesses, scenario A does not offer a valid explanation for the NANOGrav data up to $v_s = 1000$ TeV, and the resulting GW spectrum can surpass the SKA sensitivity curve at low frequencies. Scenario B provides a marginal explanation

Table 2. Summary of model parameters and prior ranges. Bayesian factors, $\text{BF}_{Y,X}$, with Y representing scenario B and X denoting SMBHB.

	m_{h_1} (GeV)	m_{h_2} (GeV)	$m_A = m_{H^\pm}$ (GeV)	m_{12}^2 (GeV) ²	$\tan\beta$	s_1	s_2	s_3	v_s (100 TeV)	λ_6	$\log_{10}(f_{\text{peak}})$	$\text{BF}_{Y,X}$
scenario B	95.4	125.5	410	550	12	0.16	0.004	0.035	Uniform [5, 10]	Uniform [0.0001, 0.0004]	Uniform [-9, -7]	22.41 ± 6.75

**Fig. 9.** (color online) Corner plot of the posterior distributions of the parameters with the 1σ (dark) and 2σ (light) credible regions. The diagonal plots are the marginalized 1D distributions with the vertical lines indicating the 68% and 95% confidence level intervals.

of the diphoton and $b\bar{b}$ excesses at 95.4 GeV at the 1σ level, but it can simultaneously offer a good explanation for the NANOGrav data.

Our work highlights the complementary roles of collider signals and GW observables in probing the nature of the extended Higgs sector. Although the 95.4 GeV excess reported by CMS, ATLAS, and LEP has not yet reached the discovery level of statistical significance, its consistent appearance across multiple experiments has inspired extensive theoretical interest, making it a well-motivated phenomenon to investigate. To our knowledge, our work is the first to simultaneously explain both the NANOGrav data and the 95.4 GeV Higgs boson excess, realized here within a coherent N2HDM framework. We explicitly identify specific scenario within the N2HDM in which this dual explanation can be realized. Our work extends previous studies of the N2HDM by connecting collider and cosmological phenomena.

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