# Impact on the magnetic compressor due to $\mathbf{CSR}^*$

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**Abstract** When an electron bunch is compressed in a chicane compressor, the CSR (coherent synchrotron radiation) will induce energy redistribution along the bunch. Such energy redistribution will affect the longitudinal emittance as a direct consequence. It will also excite betatron oscillation due to the chromatic transfer functions, and hence a transverse emittance change. So, it is indispensable for us to find a way to alleviate the CSR-caused emittance dilution and the bad result of chicane compressor in PKU-FEL.

Key words coherent synchrotron radiation, magnetic compressor, energy spread, emittance

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## 1 Introduction

Peking University IR-FEL (Infrared Free Electron Laser) Facility<sup>[1]</sup> is supported by 973 projects. It is composed of four parts: the DC-SC (direct current and superconducting) photo-injector<sup>[2]</sup>, the  $2 \times 9$  cell 1.3 GHz main accelerator, the chicane compressor<sup>[3]</sup> and the wiggler. To get a short saturation length and high luminosity FEL laser, a high luminosity electron source is needed. For the presence of space charge effect, usually, a low peak current electron beam is produced from the source first, then it is accelerated to relativistic energy, with manipulation of the phase space in the following transport line, finally we get a short electron beam and a high peak current. Chicane compressor is used in several labs to achieve short  $bunch^{[4-6]}$ . Fig. 1 shows the schematic plot of chicane compressor at Peking University.



Fig. 1. The schematic of magnetic compressor in PKU-FEL.

Before the chicane, the electron bunch has high energy in the rear and low energy in the head. In the chicane, low energy electrons will take a longer trajectory so that the bunch length gets compressed. Table 1 shows the optimized parameters of chicane compressor.

Table 1. Parameters of the magnetic compressor in PKU-FEL.

parameter	value	unit
$B_{\max}$	0.1873	Т
bend angle	12 - 22	degrees
bend effective length	20	$^{\mathrm{cm}}$
drift length between	40	$^{\mathrm{cm}}$
magnets $1-2$ and $3-4$		
drift length between magnets 2—3	20	$^{\mathrm{cm}}$
magnet gap	2.4	$^{\mathrm{cm}}$
good field of magnets 2—3	14	$^{\mathrm{cm}}$
good field of magnets 1—4	6	$^{\mathrm{cm}}$
field uniformity	0.1%	
stability of power supply	0.05%	

## 2 Energy spread

To analyze the CSR effects, we use one dimensional "steady model"<sup>[7]</sup>. The charge distribution is described by a linear Gaussian function

$$\lambda(s) = \frac{N}{\sqrt{2\pi\sigma_s}} \mathrm{e}^{-s^2/2\sigma_s^2} , \qquad (1)$$

The power loss due to CSR in different positions is

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$$\frac{\mathrm{d}\varepsilon}{\mathrm{c}\mathrm{d}t} = \frac{2Ne^2}{\sqrt{2\pi}(3\rho^2\sigma_s^4)^{1/3}}F\left(\frac{s}{\sigma_s}\right).$$
(2)

Here F is the form factor of CSR

$$F(\xi) = -\int_{-\infty}^{\xi} \frac{\mathrm{d}\xi'}{(\xi - \xi')^{1/3}} \frac{\mathrm{d}}{\mathrm{d}\xi'} \mathrm{e}^{-\xi'^2/2} , \qquad (3)$$

N is the number of electrons of the bunch;  $\rho$  is the radius of the electron trajectory; s is longiludinal coordinate;  $\sigma_s$  is the rms bunch length. It is obvious that the CSR effect becomes stronger when the bunch length gets shorter. With the CSR effect, the bunch will gain energy in the head (F > 0) and lose energy in the middle and tail  $(F < 0)^{[8]}$ . It is clear from the CSR wake potential of electron bunch shown in Fig. 2 in which the horizontal axis represents the displacement from the beam center in unit of longitudinal sigma of the bunch.



Fig. 2. CSR wake potential of electron bunch.

Before entering the chicane, the bunch is accelerated off-crest in the RF module so that the near linear chirp with the high energy tail and the low energy head is induced. When compressed in the chicane, the low energy head will gain energy but the high energy tail will lose energy, and its energy spread will become smaller due to the CSR effect!

With the simulation using ELEGANT<sup>[9]</sup>, we can see the energy spread change in the chicane compressor in Fig. 3: The energy spread changes from 4.80% to 4.74%. This is consistent with the result: The energy spread becomes smaller due to the CSR effect in the chicane compressor. The FEL lasing process will benefit from it in some sense since the low energy spread is desirable.



Fig. 3. Change of energy in the magnetic compressor.

## 3 Transversal emittance

For the edge field of dipole and without normal incidence of electron beam, the symmetric four-dipole chicane is not achromatic. The initial energy spread and the change due to CSR will affect the transversal emittance through chromatic equations<sup>[10]</sup>:  $\partial x/\partial \delta = R_{16}$ ,  $\partial x'/\partial \delta = R_{26}$ , the result is emittance dilution. The transversal emittance after compression should be

$$\varepsilon^{2} \approx \varepsilon_{0}^{2} + \varepsilon_{0} \frac{1}{\beta} \left[ \langle \Delta x^{2} \rangle + \left( \alpha \left\langle \Delta x^{2} \right\rangle^{\frac{1}{2}} + \beta \left\langle \Delta x'^{2} \right\rangle^{\frac{1}{2}} \right)^{2} \right], \tag{4}$$

Here,

$$\langle \Delta x^2 \rangle = \left( \int R_{16} \frac{\mathrm{d}\sigma_{\delta}}{\mathrm{d}s} \mathrm{d}s \right)^2, \quad \langle \Delta x'^2 \rangle = \left( \int R_{26} \frac{\mathrm{d}\sigma_{\delta}}{\mathrm{d}s} \mathrm{d}s \right)^2.$$

 $\sigma_{\delta}$  is the relative energy spread,  $\varepsilon_0$  is the initial emittance,  $\alpha$  and  $\beta$  are the twiss parameters after chicane.

The emittance change is shown in Fig. 4 also using ELEGANT. The emittance in x and y direction will both increase after the beam compressed in chicane compressor. It is a little hard to tell the difference of emittance in x before and after compressor due to the bigger scale of Fig. 4(a). Exact values of emittance will be given next.



The CSR effect was considered in those simulations. Also simulations without CSR were done to check how much the impact was. The comparison with and without CSR is shown in Table 2. The emittance in x will increase dramatically with CSR because chicago compressor is in x plane. The rela-

because chicane compressor is in x plane. The relative emittance change reaches up to 14.2%. Once the emittance causes any trouble on lasing, lots of attention should be paid to the CSR effect in the chicane.

Table 2. Emittance with and without CSR.

property	initial	final beam	final beam
	beam	(CSR OFF)	(CSR ON)
emit, $x$	$4.424~\mathrm{mm}{\cdot}\mathrm{mrad}$	$4.424~\mathrm{mm}{\cdot}\mathrm{mrad}$	$5.407~\mathrm{mm}{\cdot}\mathrm{mrad}$
emit, $y$	$3.497~\mathrm{mm}{\cdot}\mathrm{mrad}$	$3.503~\mathrm{mm}{\cdot}\mathrm{mrad}$	$3.498~\mathrm{mm}{\cdot}\mathrm{mrad}$

#### 4 Impact on compression

The energy redistribution during the chicane will destroy the linear chirp of the bunch, and cause distortion in the longitudinal phase space. With simulation, the bunch length will be compressed from 1.770 mm (5.9 ps) to 0.0956 mm (319 fs) without CSR and to 0.0975 mm (325 fs) with CSR.

## 5 Suppression of CSR

The radiation from electron bunch going through dipole comprises incoherent and coherent synchrotron radiation. If  $\lambda < \sigma_s$ , it's incoherent radiation;  $\lambda > \sigma_s$ , it's coherent radiation. Choosing a right size for the vacuum chamber is the way to suppress coherent radiation. With the shielding of chamber, strong radiation only remains in a certain wavelength range  $\sigma_s < \lambda < \lambda_c$ .  $\lambda_c$  is the characteristic wavelength, radiation beyond it will be considerably reduced<sup>[11]</sup>.

#### References

- DING Y T. Physical Study and Optimizing Design of PKU SASE FEL. Doctoral Thesis. Beijing: Peking University, 2004
- 2 HAO Jian-Kui, QUAN Sheng-Wen, XIANG Rong, ZHU Feng. High Power Laser and Particle Beams, 2002, 14(3): 456
- 3 LIU Chu-Yu, XIA Guo-Xing, ZHUANG Jie-Jia, ZHAO Kui. High Power Laser and Particle Beams, 2006, 18(1): 139
- 4 Bentson L, Emma P, Krejcik P. A New Bunch Compressor Chicane for the Slac Linac to Produce 30-fsec, 30-ka, 30-gev Electron Bunches. EPAC2002. Paris, France, 2002. 682—685
- 5 Limberg T, Piot Ph, Stulle F. Design and Performance Simulation of the ttf-fel ii Bunch Compression System.

 $\lambda_c = 2h \left(\frac{h}{\rho}\right)^{1/2}$ , *h* is the height of vacuum chamber. Considering the dispersion of electron bunch in the chamber and emittance dilution in the chicane, we decide the height of chamber to be h = 1.8 cm, then  $\lambda_c = 6.50$  cm (R = 0.553 m). The bunch quality will be kept acceptable for lasing.

### 6 Conclusion

With the simulation of ELEGANT, we know that the main cause of emittance dilution in chicane is the CSR effect which will affect the compression result also. Suppressing CSR should always be in mind when designing the chamber.

EPAC2002. Paris, France, 2002. 811-813

- 6 Borland M, Lewellen J, Milton S. A Highly Flexible Bunch Compressor for the Aps Leutl Fel. linac2000. Monterey, California, 2000
- 7 Murphy J B, Krinsky S, Gluckstern R L. Longitudinal Wakefield for an Electron Moving on a Circular Orbit. BNL-63090. April 1996
- 8 Dohlus M, Limberg T. Nucl. Instrum. Methods A, 1998, 407: 278
- 9 Borland M. http://www.aps.anl.gov/asd/oag/oagPackages. shtml#elegant
- 10 Emma P, Brinkmann R. Emittance Dilution Through Coherent Energy Spread Generation in Bending Systems. PAC1997. Hamburg, Germany, 1997, 1679—1681
- 11 Robert L. Warnock. Shielded Coherent Synchrotron Radiation and its Possible Effect in the Next Linear Collider, WWW.SLAC-PUB-5523